



Machine Learning

Learning from Data

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LECTURE 1

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Association Rule Mining – Apriori Example

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Webinar, ON4OFF Project Meeting



UNIVERSITY OF ICELAND
SCHOOL OF ENGINEERING AND NATURAL SCIENCES
FACULTY OF INDUSTRIAL ENGINEERING,
MECHANICAL ENGINEERING AND COMPUTER SCIENCE



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HELMHOLTZAI

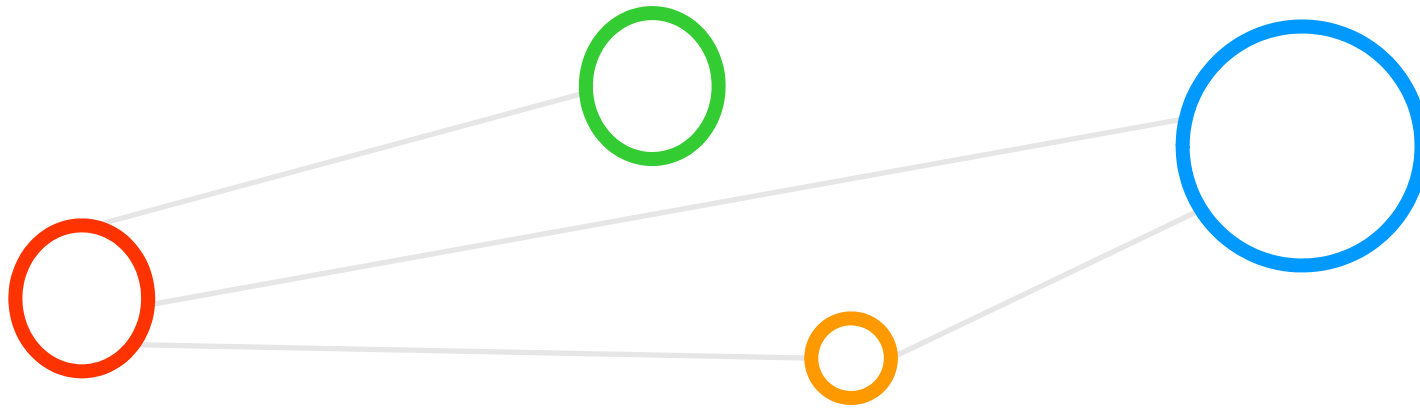
ARTIFICIAL INTELLIGENCE
COOPERATION UNIT

Outline

- Introduction to Association Rule Mining
 - Machine Learning Prerequisites & Methodology
 - Role of Datasets & Famous Dataset Example
 - Challenges & Limits in Reality
 - Support, Confidence, Lift, Leverage & Conviction Algorithm Options
 - Relevant Rules & Practical Approach
- Practical Apriori Example 'Pieper Store'
 - Apriori Algorithm & Association Rules
 - Using Python Mlxtend Library
 - Jupyter Notebook Demonstration
 - Fake Data(!) created from Supermarket Data
 - Examples in Context



Association Rule Mining



Machine Learning Prerequisites & Challenges

1. Some pattern exists
2. No exact mathematical formula
3. Data exists

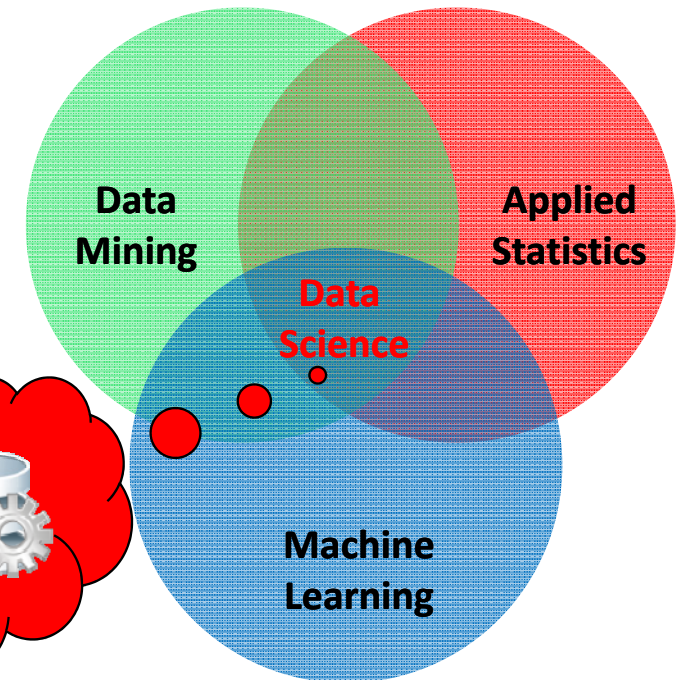
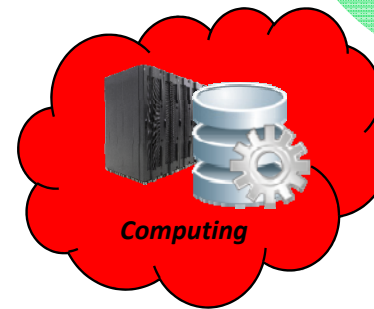
■ Idea 'Learning from Data'

- Shared with a wide variety of other disciplines
- E.g. signal processing, data mining, etc.

■ Association Rule Mining needs data!

■ Challenges

- Data is often complex
- Learning from data requires processing time → Clouds



- Machine learning is a very broad subject and goes from very abstract theory to extreme practice ('rules of thumb')
- Training machine learning models needs processing time

Association Rule Mining – Methodology

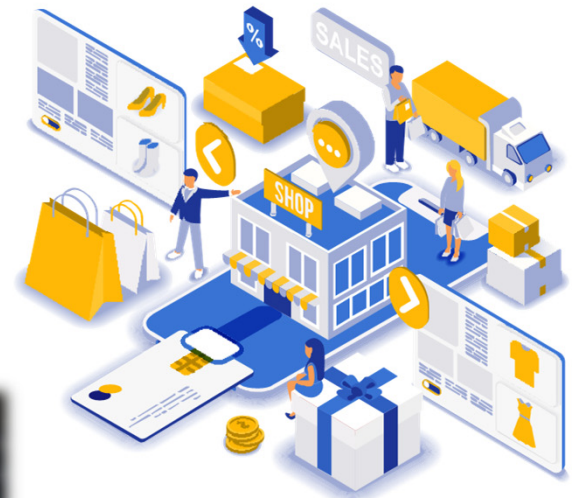
■ Methodology

- Sometimes referred to as simply 'Association Rules'
- Used to **discover unknown relationships** hidden in datasets
- **Rules** refer to a set of identified **frequent itemsets** that represent the uncovered relationships in datasets
- Identify rules that will predict the **occurrence of one or more items based on the occurrences of other items** in the dataset

■ Approach

- **Unsupervised** machine learning method
- No direct guiding output data is given to find the patterns
- **Several algorithms exist** to perform association rule mining (e.g., **Apriori**, FP Growth, MAFIA, etc.)

(this lecture will focus on Apriori with a simple demonstration)



[1] Big Data Tips,
Association Rules

Association Rule Mining – Role of Datasets

- Commercial Environments
 - Large quantities of data are **accumulated in databases** from day-to-day operations
 - Lays the foundation for mining association rules: **no data – no association rule mining!**
- Retail Example
 - **Customer purchase data** are collected on a daily basis at the **checkout counters of city stores or when shopping at online stores**
 - Accumulated data items are often **market basket transactions**
- Motivation to Collect and Analyze Data
 - Managers of stores are interested in analyzing the collected data in order to **learn the purchasing behaviour of customers**
 - Enables a **large variety of business-related applications** based on the identified rules in the data (to be reviewed from store managers!)

ON 4 OFF

(careful: can be different shopping patterns offline vs. online)



[1] *Big Data Tips, Association Rules*

Association Rule Mining – Famous Dataset Example & Challenges

■ Famous Example in Retail

- Illustrating a rule based on a strong relationship between the sale of Diapers and the sale of Beer
- Many customers who buy Diapers also buy Beer
- Investigating the transactions to find those frequent itemsets seems to be easy

■ Challenges

- In real datasets **millions or billions of transactions** are searched
- Transaction search across **100000 of different items** that may identify **1000 of rules**

■ Algorithms Benefit

- **Automation** of the process using association rule mining algorithms.
- Rules help to **identify new opportunities** and ways for **cross-selling products** to customers

ID	Items
1	{Bread, Milk}
2	{Bread, Diapers, Beer, Eggs}
3	{Milk, Diapers, Beer, Cola}
4	{Bread, Milk, Diapers, Beer}
5	{Bread, Milk, Diapers, Cola}
...	...

market basket transactions

{Diapers, Beer} Example of a frequent itemset
{Diapers} → {Beer} Example of an association rule

[1] Big Data Tips, Association Rules

Association Rule Mining – Famous Dataset Example & Limits

■ Frequent Itemsets Limits

- Very simple method
- E.g., **no personalized shopping** behaviour
- **Ignores other relevant attributes**
- E.g., **quantity** of items sold, the **price**, or even a **specific brand of items**

■ Computational Complexity

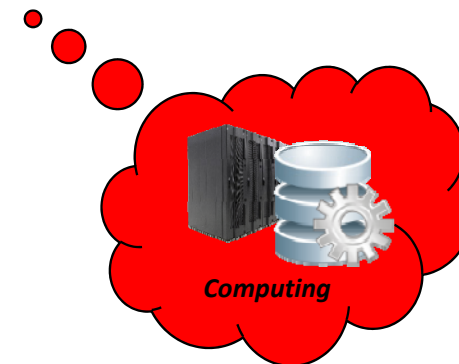
- **Mining process to discover unknown patterns** in large transaction datasets is computationally expensive
- **Size of the millions or billions of the transaction dataset** when performing mining within memory can be tricky
- **Limits with sub-sampling** of dataset items since this may increase the risk to overlook frequent itemset patterns
- E.g., use **smart out-of-cpu strategies** to work on the big datasets as a whole to identify frequent itemsets and/or use **High Performance Computing (HPC)**

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market basket transactions

{Diapers, Beer} Example of a frequent itemset

{Diapers} → {Beer} Example of an association rule



Association Rule Mining – Reality & Configuration Options

- Facing Reality in Retail Shopping
 - Some uncovered patterns are simply not true
 - Reasoning: they have happen by chance!
- Approaches
 - Manual post-processing or even application domain knowledge to find true rules out of the undiscovered patterns
 - Important is to find actionable insights from rules that can be used to change a product portfolio, store setup, or customer relations
- Configuration Options
 - In order to provide a more clear set of rules
 - E.g. support, confidence

(actionable insight:
change a product portfolio)



[2] Image:
Luehrmann.de

(actionable insight:
change a store setup)



(actionable insight:
change customer relations)



Association Rule Mining – Understanding Support Option

■ Practical Example

- Text analysis

■ Example ‘Dog’

- Appears in 7 baskets
- Not in (5)
- Support is 7

■ Example ‘Cat’

- Appears in 6 baskets
- Not (4) and (8)
- Support is 6

■ Example ‘support threshold’

- Pick $s = 3$ results in ‘5 frequent singleton itemsets’

(‘Example of 8 baskets consisting of items as words’)

1. {Cat, and, dog, bites}
2. {Yahoo, news, claims, a, cat, mated, with, a, dog, and, produced, viable, offspring}
3. {Cat, killer, likely, is, a, big, dog}
4. {Professional, free, advice, on, dog, training, puppy, training}
5. {Cat, and, kitten, training, and, behavior}
6. {Dog, &, Cat, provides, dog, training, in, Eugene, Oregon}
7. {“Dog, and, cat”, is, a, slang, term, used, by, police, officers, for, a, male-female, relationship}
8. {Shop, for, your, show, dog, grooming, and, pet, supplies}

(Basket #4 has 2x training: as baskets are modelled as sets this can be ignored)



- Careful: MLxtend implementation `min_support` threshold is set to 0.5 (50%), a frequent itemset is defined as a set of items that occur together in at least 50% of all transactions in the database

[4] *mlxtend lib, Apriori*

[5] *Mining Large Datasets*

Association Rule Mining – Understanding Support Option

■ Metrics

- Evaluating association rules and setting selection thresholds
- Given a rule "A -> C"
 - *A* stands for antecedent and *C* stands for consequent

■ Support – Revisited

- Defined for itemsets, not association rules

■ Example MLxtend lib

- Table produced by the association rule mining algorithm contains three different support metrics
- 'antecedent support' computes the proportion of transactions that contain the antecedent A
- 'consequent support' computes the support for the itemset of the consequent C
- 'support' metric then computes the support of the combined itemset A U C

ID	Items
1	{Bread, Milk}
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market basket transactions

{Diapers, Beer} Example of a frequent itemset
{Diapers} → {Beer} Example of an association rule

$$\text{support}(A \rightarrow C) = \text{support}(A \cup C), \quad \text{range: } [0, 1]$$

Typically, support is used to measure the abundance or frequency (often interpreted as significance or importance) of an itemset in a database. We refer to an itemset as a "frequent itemset" if you support is larger than a specified minimum-support threshold. Note that in general, due to the *downward closure* property, all subsets of a frequent itemset are also frequent.



[6] MLxtend Lib,
Association Rules

Association Rule Mining – Understanding Confidence Option

■ Approach

- Finding Association Rules with **high confidence** important
- Identifying useful association rules is not much harder than finding frequent itemsets

■ Practical insights

- Looking for association rules $I \rightarrow J$ that apply to a reasonable fraction of the baskets: the support of I must be **reasonably high**
- Marketing in brick-and-mortar stores **w.r.t support**: ‘**reasonably high**’ is often around 1% of the baskets
- **Confidence of the rule** should be reasonably high, e.g. 50% (otherwise the rule has little practical effect)
- As a result, the set $I \cup J$ will also have fairly high support.

ID	Items
1	{Bread, Milk}
2	{Bread, Diapers, Beer, Eggs}
3	{Milk, Diapers, Beer, Cola}
4	{Bread, Milk, Diapers, Beer}
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...	...

market basket transactions

{Diapers, Beer} Example of a frequent itemset
{Diapers} → {Beer} Example of an association rule

(Finding within all the association rules those that have both high support and high confidence is possible)

[5] Mining Large Datasets

Association Rule Mining – Understanding Confidence & Lift Option

■ Example MLxtend lib – Confidence

- **Confidence** of a rule $A \rightarrow C$ is the probability of seeing the consequent in a transaction given that it also contains the antecedent
- Metric is not symmetric or directed
- E.g, the confidence for $A \rightarrow C$ is different than the confidence for $C \rightarrow A$
- Confidence is 1 (maximal) for a rule $A \rightarrow C$ if the consequent and antecedent always occur together

ID	Items
1	{Bread, Milk}
2	{Bread, Diapers, Beer, Eggs}
3	{Milk, Diapers, Beer, Cola}
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market basket transactions

{Diapers, Beer} Example of a frequent itemset
 {Diapers} → {Beer} Example of an association rule

■ Example MLxtend lib – Lift

- **Lift** metric is commonly used to measure how much more often the antecedent and consequent of a rule $A \rightarrow C$ occur together than we would expect if they were statistically independent
- E.g., if A and C are independent, the Lift score will be exactly 1

$$\text{confidence}(A \rightarrow C) = \frac{\text{support}(A \rightarrow C)}{\text{support}(A)}, \quad \text{range: } [0, 1]$$

$$\text{lift}(A \rightarrow C) = \frac{\text{confidence}(A \rightarrow C)}{\text{support}(C)}, \quad \text{range: } [0, \infty]$$

[6] MLxtend Lib,
Association Rules

Association Rule Mining – Understanding Leverage & Conviction Option

■ Example MLxtend lib – Leverage

- **Leverage** computes the difference between the observed frequency of A and C appearing together and the frequency that would be expected if A and C were independent
- An leverage value of 0 indicates independence

ID	Items
1	{Bread, Milk}
2	{Bread, Diapers, Beer, Eggs}
3	{Milk, Diapers, Beer, Cola}
4	{Bread, Milk, Diapers, Beer}
5	{Bread, Milk, Diapers, Cola}
...	...

market basket transactions

{Diapers, Beer} Example of a frequent itemset
 {Diapers} → {Beer} Example of an association rule

$$\text{leverage}(A \rightarrow C) = \text{support}(A \rightarrow C) - \text{support}(A) \times \text{support}(C), \quad \text{range: } [-1, 1]$$

■ Example MLxtend lib – Conviction

- **High conviction** value means that the consequent is highly depending on the antecedent
- E.g., in the case of a perfect confidence score, the denominator becomes 0 (due to 1 - 1) for which the conviction score is defined as 'inf'
- Similar to lift, if items are independent, the conviction is 1

$$\text{conviction}(A \rightarrow C) = \frac{1 - \text{support}(C)}{1 - \text{confidence}(A \rightarrow C)}, \quad \text{range: } [0, \infty]$$

[6] MLxtend Lib, Association Rules

Relevant Rules & Practical Approach

■ Relevant Rules

- Assumed that there are not too many frequent itemsets
- Not many candidates for high-support, high-confidence association rules.

■ 'less is more'

- Each one found from above must be acted upon
- If store manager receives a million association rules that meet thresholds (e.g. for support and confidence) they cannot read them or act on them

■ Practical Approach

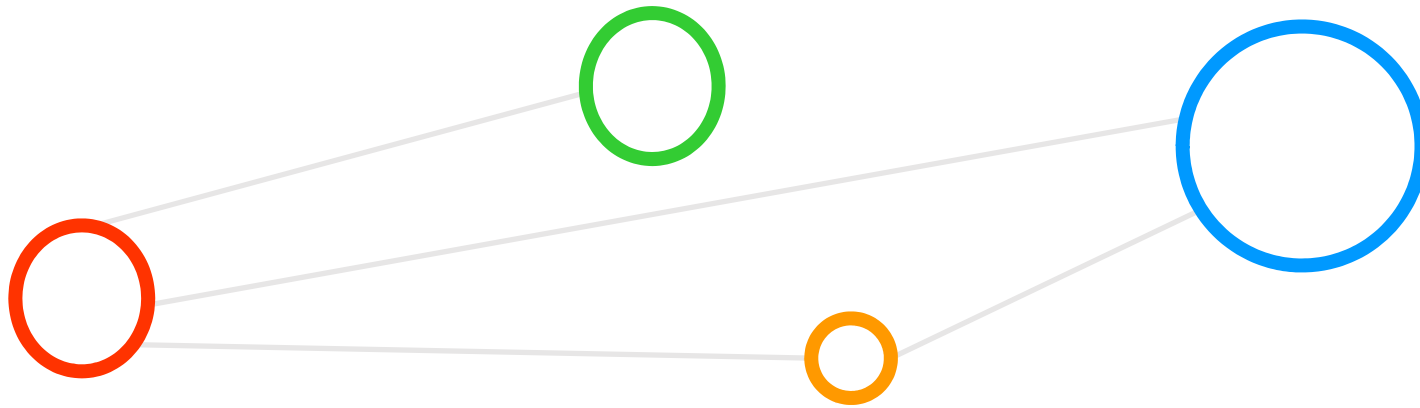
- Normal to **adjust the support threshold s**
- Provides not **'too many frequent itemsets'**
- **Implement and review with store manager step-wise to measure results better**



(Generating 'big data': Major chains might sell 100.000 different items and collect data about millions of market baskets)

- **The massive amount of data and derived rules requires an automated algorithm-based approach**
- **The most commonly used algorithm (and its variants) for association rules mining is called Apriori**

Practical Apriori Example 'Pieper Store'



Jupyter Notebook Demonstration

Association-Rule-Mining/ x association-rule-mining-apriori x +

localhost:8888/tree/Association-Rule-Mining 150%

jupyter Quit Logout

Files Running Clusters

Select items to perform actions on them. Upload New ↕

<input type="checkbox"/> 0	Name ↓	Last Modified	File size
<input type="checkbox"/>	..	vor ein paar Sekunden	
<input type="checkbox"/>	data	vor 18 Minuten	
<input type="checkbox"/>	association-rule-mining-apriori-example.ipynb	Running vor 18 Minuten	13.8 kB

Python Script using MLxtend Library

```
In [ ]: import pandas as pd
import numpy as np
from mlxtend.frequent_patterns import apriori, association_rules
import matplotlib.pyplot as plt

In [ ]: df = pd.read_csv('./data/retail_dataset-pieper-fake.csv', sep=',')
df.head()

In [ ]: items = (df['0']).unique()
items

In [ ]: # transform dataset to one-hot encoded dataset
encoded_items = []
def onehotencoding():
    for index, row in df.iterrows():
        present = {}
        uncommons = list(set(items) - set(row))
        commons = list(set(items).intersection(row))
        for uc in uncommons:
            present[uc] = 0
        for com in commons:
            present[com] = 1
        encoded_items.append(present)
onehotencoding()
ohe_df = pd.DataFrame(encoded_items)
print(ohe_df)

In [ ]: # running apriori algorithm
freq_items = apriori(ohe_df, min_support=0.2, use_colnames=True, verbose=1)
freq_items.head(7)

In [ ]: # using frequent itemsets from apriori for association rules
rules = association_rules(freq_items, metric="confidence", min_threshold=0.6)
rules.head(7)
```

*changed from
[7] MLxtend tutorial*

Pieper Store Example – Fake Data

[3] Pieper.de Duetfe

■ Retail Data

■ Original

(for simplicity we focus here on the brand names and not on the detailed description, sizes in ml, or different prices)

- 1 0, 1, 2, 3, 4, 5, 6
- 2 Bread, Wine, Eggs, Meat, Cheese, Pencil, Diaper
- 3 Bread, Cheese, Meat, Diaper, Wine, Milk, Pencil
- 4 Cheese, Meat, Eggs, Milk, Wine, ,
- 5 Cheese, Meat, Eggs, Milk, Wine, ,
- 6 Meat, Pencil, Wine, , , ,
- 7 Eggs, Bread, Wine, Pencil, Milk, Diaper, Bagel
- 8 Wine, Pencil, Eggs, Cheese, , ,
- 9 Bagel, Bread, Milk, Pencil, Diaper, ,
- 10 Bread, Diaper, Cheese, Milk, Wine, Eggs,
- 11 Bagel, Wine, Diaper, Meat, Pencil, Eggs, Cheese
- 12 Cheese, Meat, Eggs, Milk, Wine, ,
- 13 Bagel, Eggs, Meat, Bread, Diaper, Wine, Milk
- 14 Bread, Diaper, Pencil, Bagel, Meat, ,
- 15 Bagel, Cheese, Milk, Meat, , ,
- 16 Bread, , , , ,
- 17 Pencil, Diaper, Bagel, , , ,
- 18 Meat, Bagel, Bread, , , ,
- 19 Bread, Bagel, Milk, , , ,
- 20 Diaper, , , , ,
- 21 Bagel, Cheese, Meat, Bread, Diaper, Eggs,
- 22 Meat, Pencil, Cheese, Bread, , ,
- 23 Cheese, Eggs, Wine, Bread, Milk, Pencil, Meat
- 24 Eggs, Bagel, Cheese, Meat, Diaper, ,

- 1 0, 1, 2, 3, 4, 5, 6
- 2 HugoBoss, Chanel, Rituals, Armani, Biotherm, Lancome, Dior
- 3 HugoBoss, Biotherm, Armani, Dior, Chanel, Clinique, Lancome
- 4 Biotherm, Armani, Rituals, Clinique, Chanel, ,
- 5 Biotherm, Armani, Rituals, Clinique, Chanel, ,
- 6 Armani, Lancome, Chanel, , , ,
- 7 Rituals, HugoBoss, Chanel, Lancome, Clinique, Dior, Clinique
- 8 Chanel, Lancome, Rituals, Biotherm, , ,
- 9 Clinique, HugoBoss, Clinique, Lancome, Dior, ,
- 10 HugoBoss, Dior, Biotherm, Clinique, Chanel, Rituals,
- 11 Clinique, Chanel, Dior, Armani, Lancome, Rituals, Biotherm
- 12 Biotherm, Armani, Rituals, Clinique, Chanel, ,
- 13 Clinique, Rituals, Armani, HugoBoss, Dior, Chanel, Clinique
- 14 HugoBoss, Dior, Lancome, Clinique, Armani, ,
- 15 Clinique, Biotherm, Clinique, Armani, , ,
- 16 HugoBoss, , , , , ,
- 17 Lancome, Dior, Clinique, , , ,
- 18 Armani, Clinique, HugoBoss, , , ,
- 19 HugoBoss, Clinique, Clinique, , , ,
- 20 Dior, , , , ,
- 21 Clinique, Biotherm, Armani, HugoBoss, Dior, Rituals,
- 22 Armani, Lancome, Biotherm, HugoBoss, , , ,
- 23 Biotherm, Rituals, Chanel, HugoBoss, Clinique, Lancome, Armani
- 24 Rituals, Clinique, Biotherm, Armani, Dior, ,



paco rabanne

1 Million
PARFUM SPRAY

50 ml
● Sofort lieferbar € 73,50 € 47,40
€ 94,80 / 100 ml

100 ml
● Sofort lieferbar € 97,50 € 63,20
€ 63,20 / 100 ml

200 ml
● Sofort lieferbar € 134,00
€ 67,00 / 100 ml

AUF MEINEN WUNSCHZETTEL IN DEN WARENKORB

Versandkostenfrei

CHANEL
BLEU DE CHANEL
EAU DE PARFUM ZERSTÄUBER

Auswahlpreis: 120,30 €

Sofort lieferbar
€ 80,20 / 100 Milliliter

Auswahlinfo: Variante: 150 ml | Menge: 150ml

100 ml € 100,10
inkl. MwSt.

150 ml € 120,30
inkl. MwSt.

Duftbox mit 50 ml € 89,90
inkl. MwSt.

Duftbox mit 100 ml € 98,30
inkl. MwSt.

Association Rule Mining – Understanding Support Option – Revisited

- Example MLxtend lib

- Table produced by the association rule mining algorithm $\text{support}(A \rightarrow C) = \text{support}(A \cup C)$, range: [0, 1] contains three different support metrics
- 'antecedent support' computes the proportion of transactions that contain the antecedent A
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- 'support' metric then computes the support of the combined itemset A U C

	antecedents	consequents	antecedent support	consequent support	support	confidence	lift	leverage	conviction
0	(Dior)	(Clinique)	0.406349	0.701587	0.260317	0.640625	0.913108	-0.024772	0.830366
1	(Biotherm)	(Clinique)	0.501587	0.701587	0.409524	0.816456	1.163726	0.057617	1.625835
2	(HugoBoss)	(Clinique)	0.504762	0.701587	0.387302	0.767296	1.093657	0.033167	1.282368
3	(Chanel)	(Clinique)	0.438095	0.701587	0.301587	0.688406	0.981212	-0.005775	0.957697
4	(Rituals)	(Clinique)	0.438095	0.701587	0.333333	0.760870	1.084497	0.025971	1.247908
5	(Armani)	(Clinique)	0.476190	0.701587	0.358730	0.753333	1.073756	0.024641	1.209781
6	(Lancome)	(Clinique)	0.361905	0.701587	0.260317	0.719298	1.025244	0.006410	1.063095

[6] MLxtend Lib, Association Rules

Association Rule Mining – Understanding Confidence & Lift Option – Revisited

■ Example MLxtend lib – Confidence

- **Confidence** of a rule A->C is the probability of seeing the consequent in a transaction given that it also contains the antecedent
- Metric is not symmetric or directed
- E.g, the confidence for A->C is different than the confidence for C->A
- Confidence is 1 (maximal) for a rule A->C if the consequent and antecedent always occur together

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$$\text{confidence}(A \rightarrow C) = \frac{\text{support}(A \rightarrow C)}{\text{support}(A)}, \quad \text{range: } [0, 1]$$

■ Example MLxtend lib – Lift

- **Lift** metric is commonly used to measure how much more often the antecedent and consequent of a rule A->C occur together than we would expect if they were statistically independent
- E.g., if A and C are independent, the Lift score will be exactly 1

$$\text{lift}(A \rightarrow C) = \frac{\text{confidence}(A \rightarrow C)}{\text{support}(C)}, \quad \text{range: } [0, \infty]$$

[6] MLxtend Lib,
Association Rules

Association Rule Mining – Understanding Leverage & Conviction Option

■ Example MLxtend lib – Leverage

- **Leverage** computes the difference between the observed frequency of A and C appearing together and the frequency that would be expected if A and C were independent
- An leverage value of 0 indicates independence

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$$\text{leverage}(A \rightarrow C) = \text{support}(A \rightarrow C) - \text{support}(A) \times \text{support}(C), \quad \text{range: } [-1, 1]$$

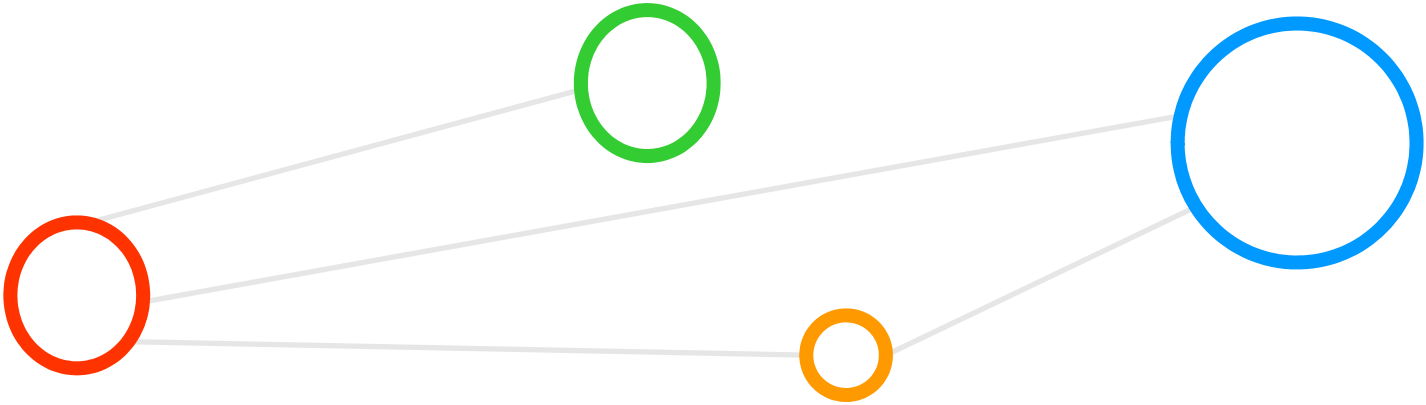
■ Example MLxtend lib – Conviction

- **High conviction** value means that the consequent is highly depending on the antecedent
- E.g., in the case of a perfect confidence score, the denominator becomes 0 (due to 1 - 1) for which the conviction score is defined as 'inf'
- Similar to lift, if items are independent, the conviction is 1

$$\text{conviction}(A \rightarrow C) = \frac{1 - \text{support}(C)}{1 - \text{confidence}(A \rightarrow C)}, \quad \text{range: } [0, \infty]$$

[6] MLxtend Lib,
Association Rules

Lecture Bibliography



Lecture Bibliography

- [1] Big Data Tips, Association Rules, Online:
<http://www.big-data.tips/association-rules>
- [2] Luehrmann.de, 'Parfuemerie Pieper bezieht markante Eckimmobilie', Online:
<https://www.luehrmann.de/de/city-life/erfolgsraume/beitrag/parfumerie-pieper-bezieht-markante-eckimmobilie/>
- [3] Pieper.de Duefte, Online:
<https://www.pieper.de/duefte/>
- [4] MLxtend Library, Apriori:
http://rasbt.github.io/mlxtend/user_guide/frequent_patterns/apriori/
- [5] Mining of Massive Datasets, Anand Rajaraman, Jure Leskovec, Jeffrey D. Ullman, Cambridge University Press, ISBN 1107015359, ~326 pages, English, 2011
- [6] MLxtend Library, Association Rules:
http://rasbt.github.io/mlxtend/user_guide/frequent_patterns/association_rules/
- [7] Tutorial, Association Analysis in Python, Online:
<https://medium.com/analytics-vidhya/association-analysis-in-python-2b955d0180c>

