

High Performance Computing

ADVANCED SCIENTIFIC COMPUTING

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SHORT LECTURE 15

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Computational Fluid Dynamics & Finite Elements

November 25, 2019

Room V02-156



UNIVERSITY OF ICELAND
SCHOOL OF ENGINEERING AND NATURAL SCIENCES
FACULTY OF INDUSTRIAL ENGINEERING,
MECHANICAL ENGINEERING AND COMPUTER SCIENCE



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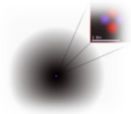
HELMHOLTZ
RESEARCH FOR GRAND CHALLENGES



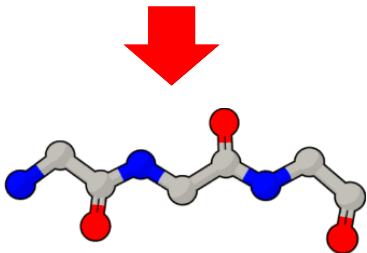
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Review of Short Lecture 14 – Molecular Systems & Libraries

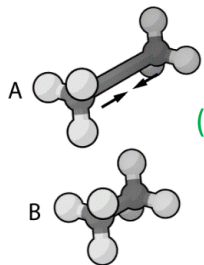
(atoms consists of 'electron cloud' & nucleus of protons and neutrons)



(molecules are a group of two or more atoms held together by chemical bonds)

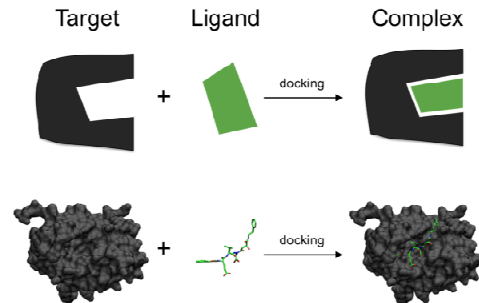


(example: molecular model of a protein)

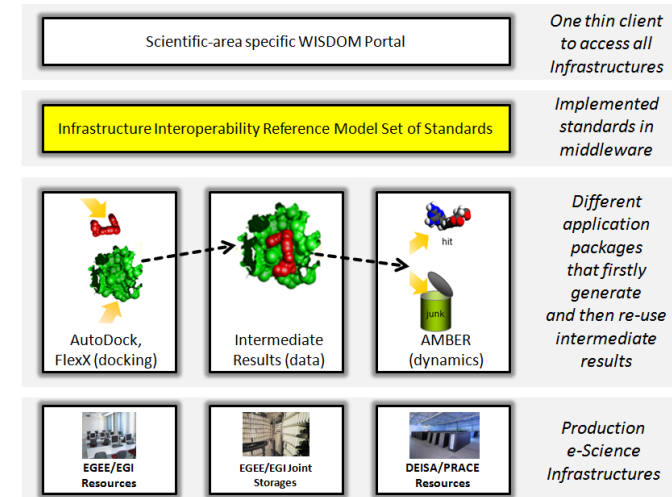
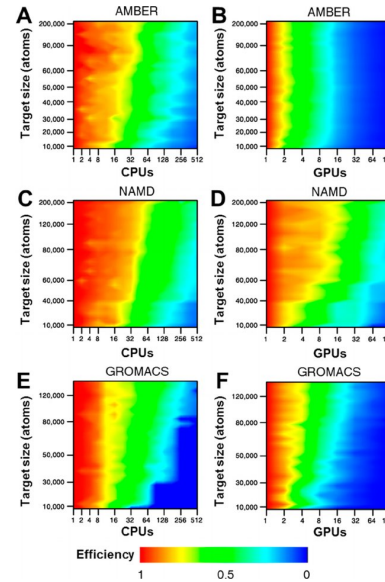
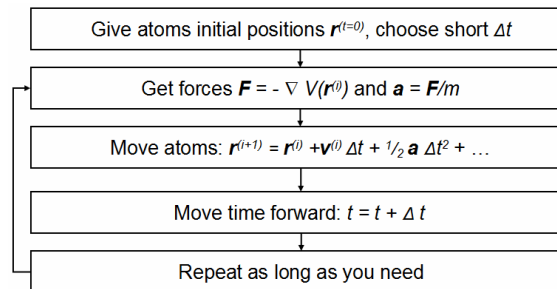


(force field)

(example: drug design with molecular docking + dynamics)



(once docked a simulation of time is useful to apply)



[7] M. Riedel et al., 'Research Advances by using interoperable e-Science Infrastructures', 2009

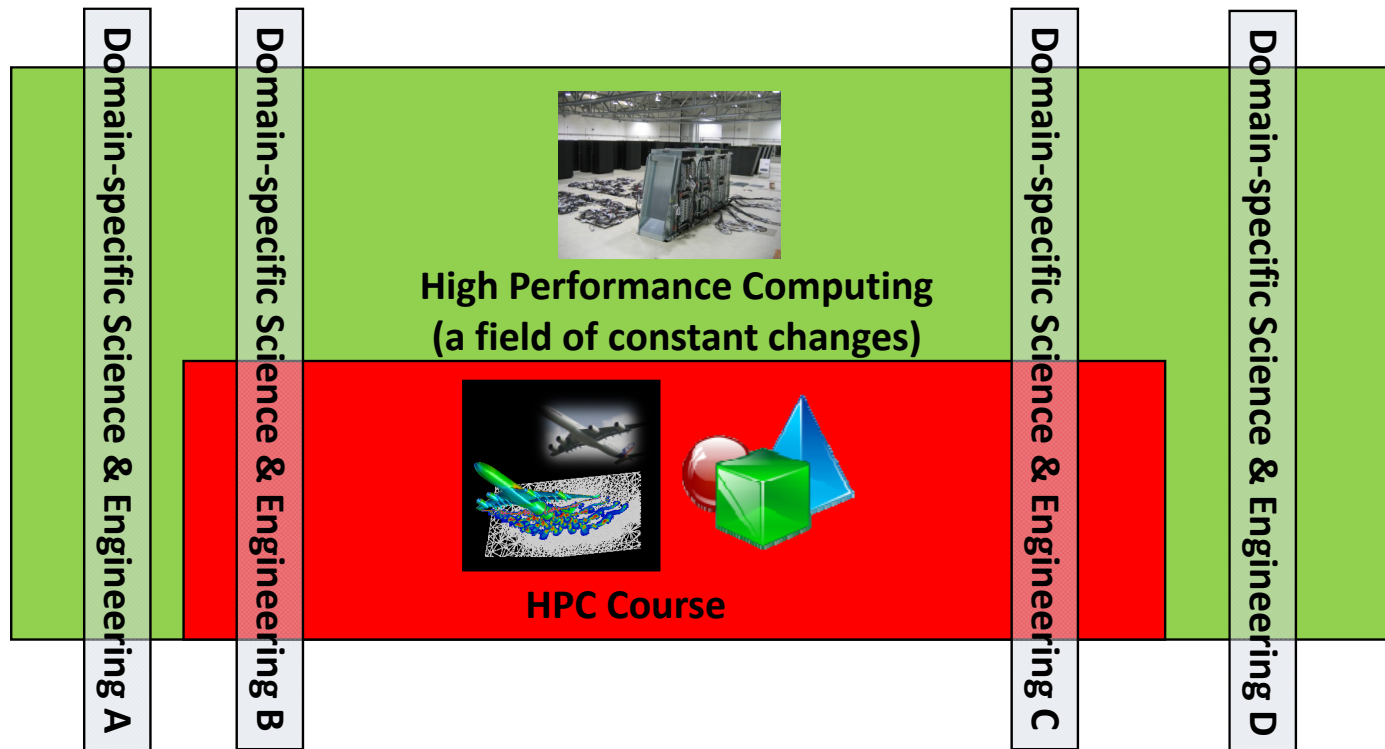
modified from [5] Wikipedia on 'Molecular Dynamics'

[6] Hu Ge et al. modified from [4] Wikipedia on 'Molecular Docking'

[3] Wikipedia on 'Molecular Mechanics' [2] Wikipedia on 'Atoms' [1] Wikipedia on 'Molecule'

HPC-A[dvanced] Scientific Computing (cf. Prologue) – Second Part

- Consists of techniques for programming & using large-scale HPC Systems
 - Approach: Get a **broad understanding what HPC is** and what can be done
 - Goal: Train **general HPC techniques and systems** and selected details of **domain-specific applications**



Outline of the Course

1. High Performance Computing
2. Parallel Programming with MPI
3. Parallelization Fundamentals
4. Advanced MPI Techniques
5. Parallel Algorithms & Data Structures
6. Parallel Programming with OpenMP
7. Graphical Processing Units (GPUs)
8. Parallel & Scalable Machine & Deep Learning
9. Debugging & Profiling & Performance Toolsets
10. Hybrid Programming & Patterns

11. Scientific Visualization & Scalable Infrastructures
12. Terrestrial Systems & Climate
13. Systems Biology & Bioinformatics
14. Molecular Systems & Libraries
15. Computational Fluid Dynamics & Finite Elements
16. Epilogue

+ additional practical lectures & Webinars for our hands-on assignments in context

- Practical Topics
- Theoretical / Conceptual Topics

Outline

■ Computational Fluid Dynamics (CFD)

- Terminology & Motivation for CFD Applications
- Navier-Stokes & Lattice-Boltzmann Method
- Large Eddy Turbulence Model
- Modelling Methodology & Application Examples
- Library Examples with OpenFOAM & iFluids

■ Finite Elements Methods (FEM)

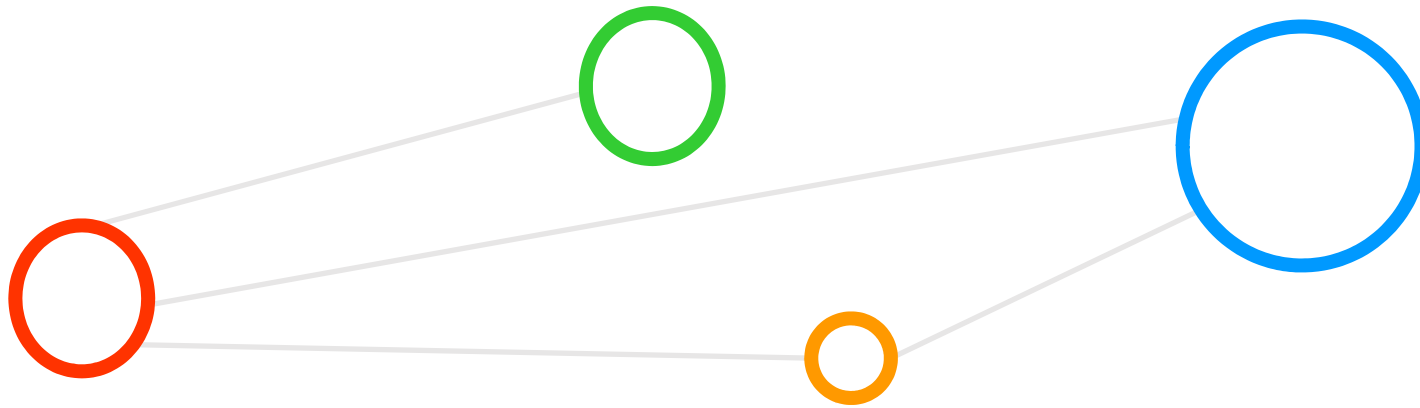
- Terminology & Motivation for FEM Applications
- Boundary Value Problems & Mesh Generation Techniques
- Adaptive Mesh Refinement & Fire Dynamics Applications
- Library Examples with OpenFOAM & Code_Aster & Ansys Suite
- Library Elmer Dynamic Ice Simulation Application Example

- Promises from previous lecture(s):
- *Lecture 2:* Lecture 12 – 15 will offer more insights into a wide variety of physics & engineering applications that take advantage of HPC with MPI
- *Lecture 3:* Lecture 15 will offer more details on HPC applications that perform computational fluid dynamics (CFD) on domain decompositions
- *Lecture 14:* Lecture 15 will give further details on computational fluid dynamics (CFD) techniques & codes including Finite Elements Method (FEM)

- Note that this lecture is only a short lecture that usually needs a full course
- The goal is to understand selected HPC application fields & provide a few pointers to other advanced related university courses/topics/tutorials



Computational Fluid Dynamics (CFD)



Computational Fluid Dynamics (CFD) – Terminology & Motivation

- ‘Fluid Dynamics’ as branch of ‘Fluid Mechanics’

- Alternative to Experimental fluid dynamics & Theoretical Fluid Dynamics
- Computational Fluid Dynamics (CFD) use numerical methods (cf. Lecture 12)
- Interaction of fluids with surfaces defined by certain boundary conditions & equations

- Usage

- Detailed product development (e.g. cars, aircraft)
- Conceptual studies of new designs
- Troubleshooting & Redesign

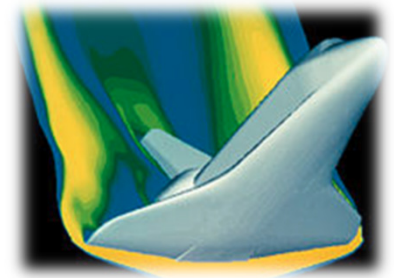
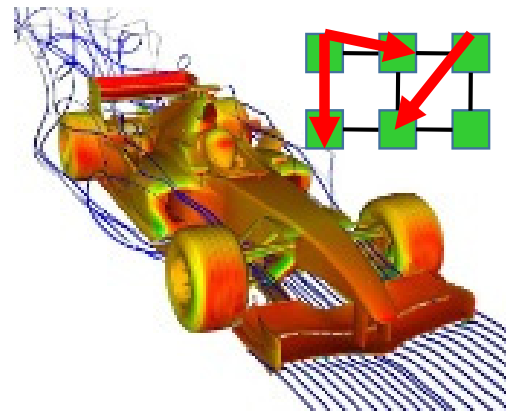
- Various Approaches

- E.g. Navier-Stokes equations, Lattice-Boltzmann method, Large-Eddy, etc.

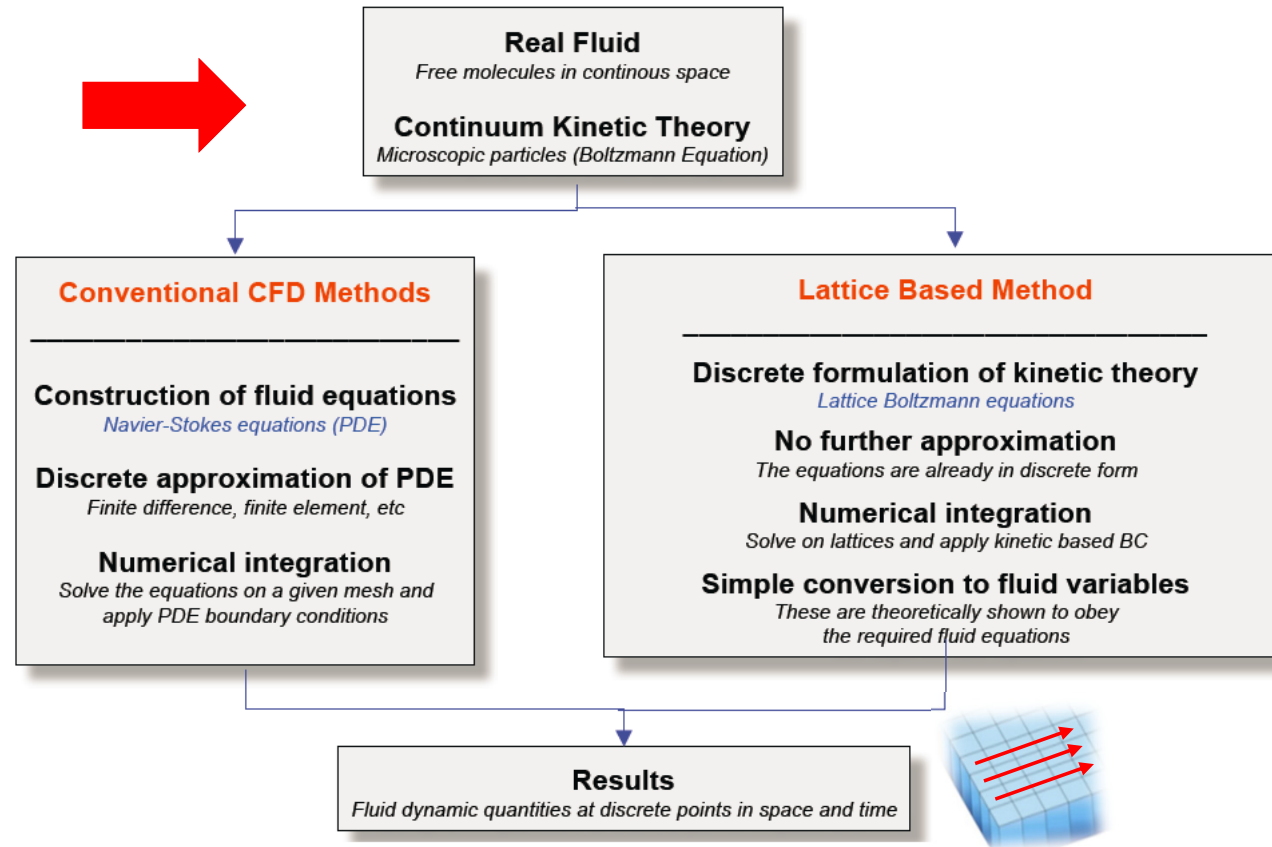
- Fluid dynamics stands for the science of fluid motion in order to understand liquids, gases, etc.
- Computational Fluid Dynamics (CFD) use numerical methods to analyze fluid flows

[8] Wikipedia on CFD

Modified from
[9] Caterham F1 team



Computational Fluid Dynamics – Methods Overview – Revisited (cf. Lecture 14)



[10] S. Orszag et al.

CFD – Navier-Stokes Method

- Origin of unique name
 - Named after Claude-Louis **Navier** and George Gabriel **Stokes**
- Solving equations
 - **Solution is a velocity** (not a position)
 - Result is a '**velocity/flow field**'
 - Description of the **velocity of the fluid** at a given point in space and time
- Modeling CFD examples
 - **Ocean currents** (cf. assignments)
 - **Water flow** in a pipe
 - **Air flow** around a wing

- **Navier-Stokes equations are used in CFD simulations to describe the motion of fluid substances**
- **Equations describe the physics of a wide variety of elements in scientific and engineering domains**

modified from [11] Wikipedia on Navier-Stokes

$$\rho \left(\frac{\partial \mathbf{v}}{\partial t} + \mathbf{v} \cdot \nabla \mathbf{v} \right) = -\nabla p + \nabla \cdot \mathbf{T} + \mathbf{f}$$

\mathbf{v} is the flow velocity,

ρ is the fluid density,

p is the pressure,

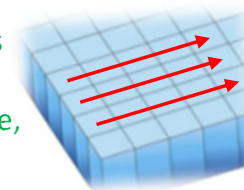
\mathbf{T} is the (deviatoric) component of the total stress tensor, which has order two,

\mathbf{f} represents body forces (per unit volume) acting on the fluid,

∇ is the del operator.

(equations are nonlinear partial differential equations - PDEs, cf. Lecture 12)

(classical mechanics solutions are rather trajectories of positions of a certain particle, here fluid velocity is in focus)



CFD – Lattice Boltzmann Method

- Alternative to Navier-Stokes
 - Different set of equations
- Modeling approach
 - Fluid consisting of particles
 - Particles have a finite number of discrete velocity values
 - Particles perform consecutive propagation and collision processes
 - Performed over discrete lattice mesh
- Modeling complex CFD examples
 - Airflow around a vehicle
 - Blood flow in a brain

(traditional CFD methods solve the conservation equations of macroscopic properties like mass, momentum, and energy)

$$f_i^t(\vec{x}, t + \delta_t) = f_i(\vec{x}, t) + \frac{1}{\tau_f}(f_i^{eq} - f_i)$$

(Collision step)

$$f_i(\vec{x} + \vec{e}_i \delta_t, t + \delta_t) = f_i^t(\vec{x}, t + \delta_t)$$

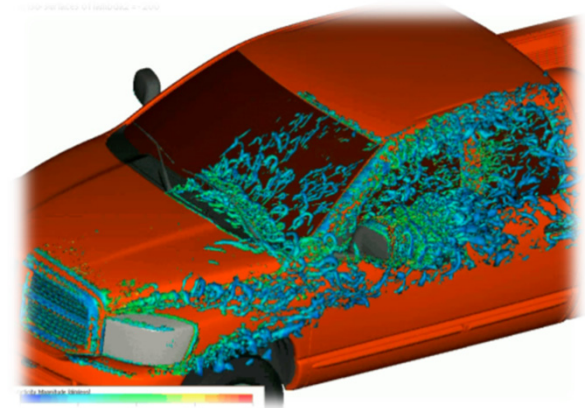
(Streaming step)

(Research acoustic impact of headlights)

[10] S. Orszag et al.

- The Lattice Boltzmann Method (LBM) is used in CFD simulations to perform fluid simulations
- Discrete Boltzmann equations are solved to simulate the flow of fluids including collision models

modified from [12] Wikipedia on LBM



CFD – Large Eddy Simulations (LES) for Turbulence

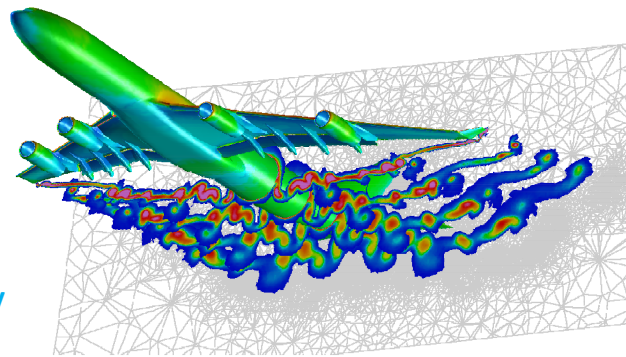
■ Simulating ‘Turbulence’

- Flow characterized by ‘chaotic property changes’ (chaotic from chaos theory)
- Low momentum diffusion
- High momentum convection
- Rapid variation of pressure and velocity (in space and time)

■ LES enables complex simulations

- Solution is a **filtered velocity field** (filtered Navier-Stokes equations)
- **Small length and time scales** enable computational simulation

[14] Wikipedia on Turbulence



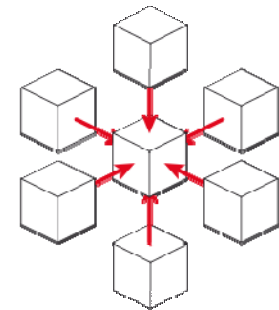
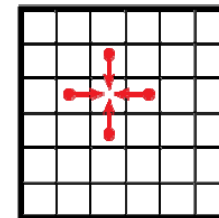
- Large Eddy Simulation (LES) is a mathematical model for turbulence used in CFD simulations
- LES operates on the Navier-Stokes equations to reduce the range of length scales of the solution

modified from [13] Wikipedia on LES



Stencil-based Iterative Methods – Revisited (cf. Lecture 10)

- Simulation sciences & numerical methods
 - **Stencil-based iterative methods**
 - Applicable with exceptions with other methods: Finite element method (selected codes on regular grids can use stencil codes)
- Selected application examples
 - Computational Fluid Dynamics (CFD) codes
 - Partial differential equations (PDE) solver
 - **Jacobi method**
 - Gauss-Seidel method
 - Image processing



- Stencil-based iterative methods update array elements according to a fixed pattern called 'stencil'
- The key of stencil methods is its regular structure mostly implemented using arrays in codes
- Method is often used in computational science as part of scientific and engineering applications

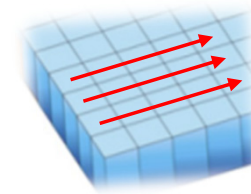
[15] Wikipedia on 'stencil code'

CFD – Modeling Methodology

- Solve practical fluid flow problems

- Modeling & simulating reality but with specific scientific detailed elements

[8] Wikipedia on CFD



- Practical Preprocessing Steps

1. Geometry (**physical bounds**) of the problem space is defined
2. Volume occupied by the fluid is divided into discrete cells (**aka 'mesh'**)
3. Physical modeling is defined (e.g. **equations of motion**)
4. Boundary conditions (e.g. **specify fluid behaviour & boundary properties**)

- Computational simulation

- Equations are **solved iteratively** via time-steps over space →

- Postprocessing Steps

- Further simulation **output data analysis** and/or visualization



Selected Libraries & Methods – OpenFOAM & iFluids

■ OpenFOAM Selected Facts

- Free and open source software & maintained by OpenFOAM foundation
- Use of object oriented programming (e.g. C++ classes, etc.)

■ OpenFOAM Parallelization

- Several methods for Domain decomposition (cf. Lecture 3)
- Distributed memory with MPI(cf. Lecture 2)

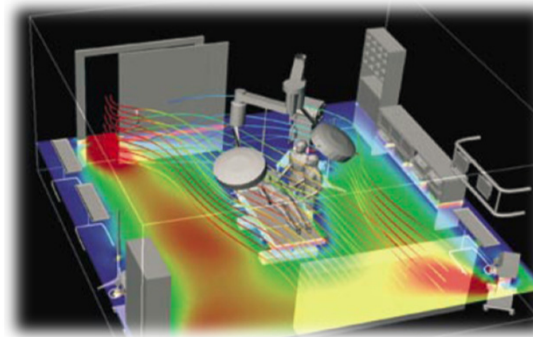
■ OpenFOAM Examples

- Dispersion of stack exhaust above a pitched roof (e.g. environmental consulting)

■ Library Example iFluids

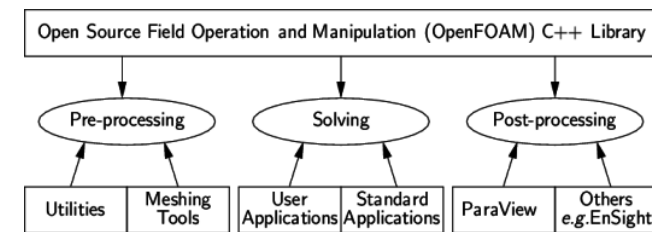
- Example for computational steering

- iFluids is a parallel software for CFD simulations in general & for indoor air flow simulations in particular being also augmented with computational steering capabilities & online visualizations

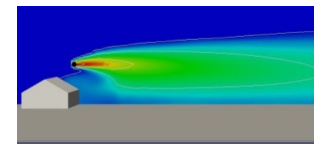
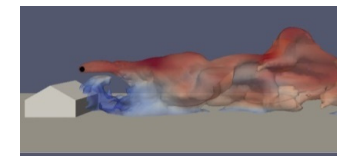


- Open source field operation & manipulation (OpenFOAM) is a C++ toolbox of numerical solvers & pre-/post processing utilities for the solution of CFD problems used in HPC simulations

modified from [32] OpenFOAM Web page



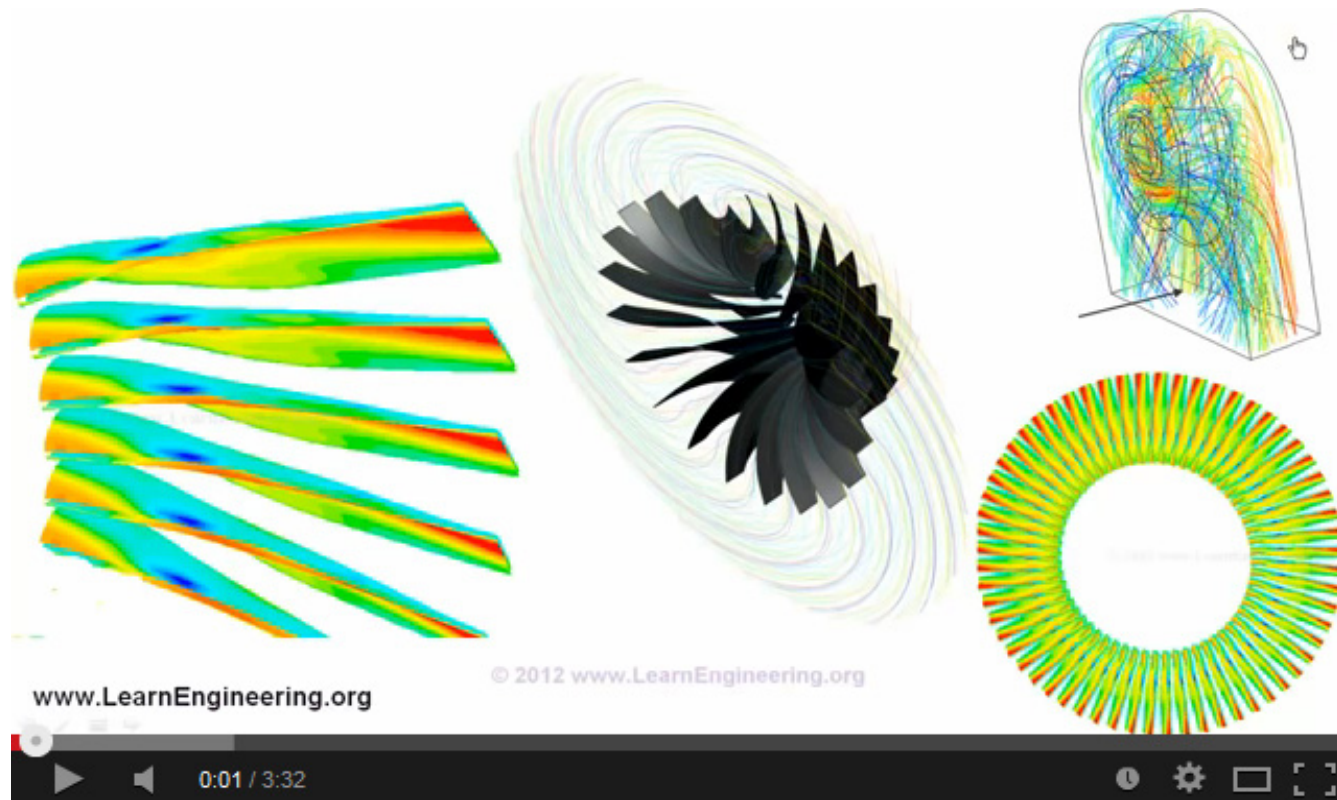
(Parallelization is inherent in the OpenFOAM design)



(using the LES mode within OpenFOAM)

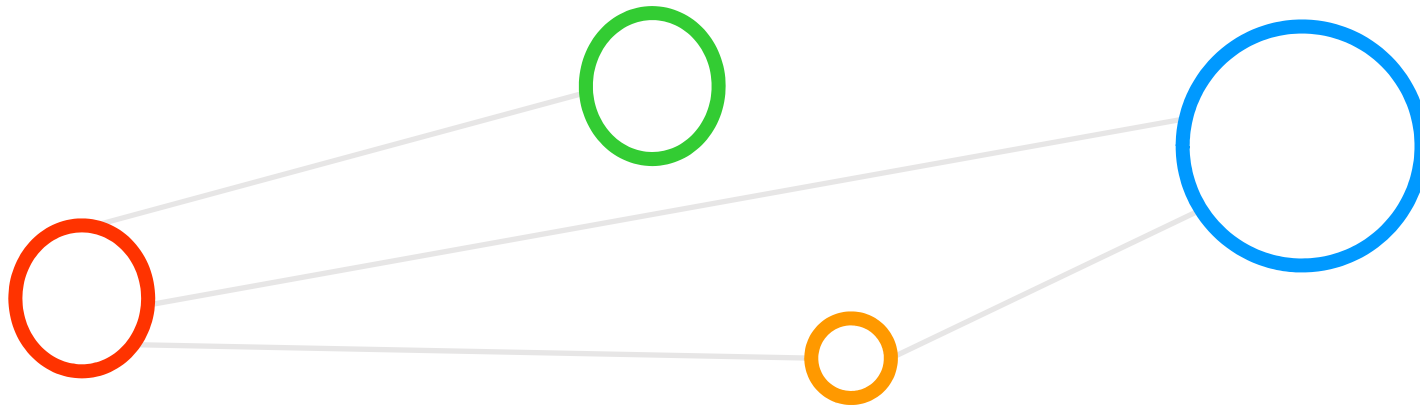
[33] P. Wenisch et al. [31] Lohmeier Consulting Engineers

[Video] CFD Summary



[16] YouTube Video, CFD

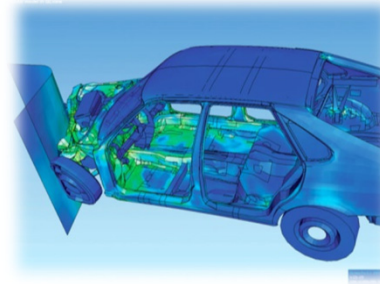
Finite Elements Method (FEM)



Finite Elements Methods (FEM) – Terminology & Motivation

■ Approach

- Approximate 'complex equations over a large domain' (i.e. resulting mesh)
- Connecting many simple element equations over many small subdomains (i.e. finite elements)
- Fixed vs. dynamic domain decompositions

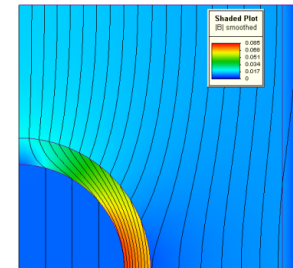
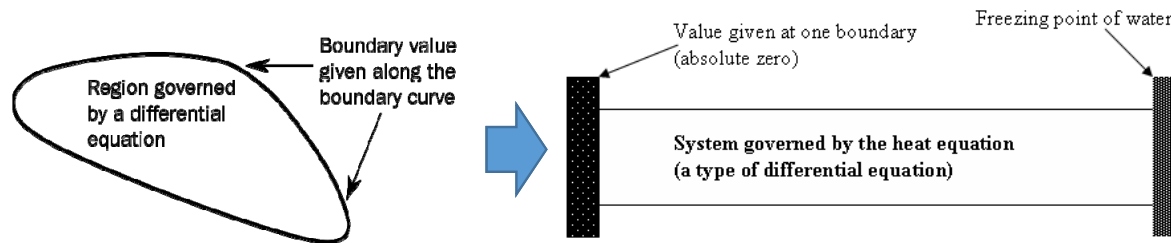


- Finite Elements Methods (FEM) is a numerical method to find approximate solutions to boundary value problems (governed by partial differential equations) by connecting many simple elements

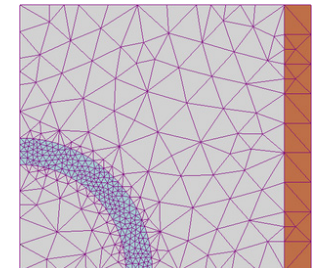
[19] Wikipedia on FEM

■ Boundary value problems

- Boundary outlines a region governed by partial differential equations (PDEs)



[18] Wikipedia on Boundary value problems



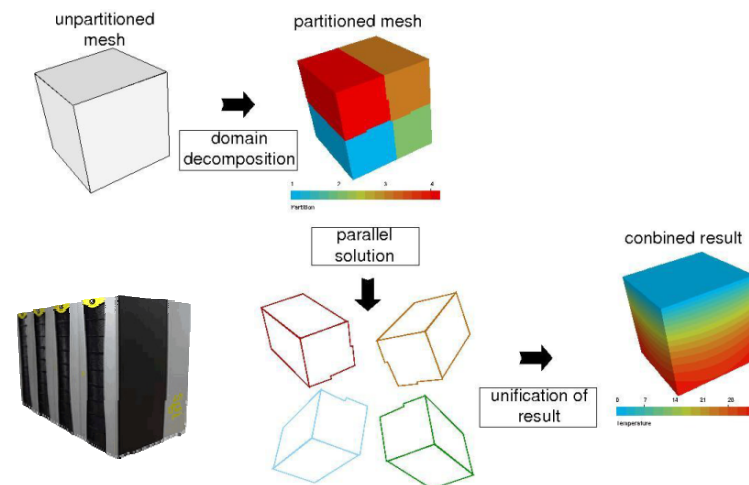
(FEM mesh to solve a magnetic problem)

FEM – Mesh Generation Technique

- Practice ‘mesh creation’
 - Tools offer the creation of meshes in a straightforward way
 - For large complex geometry objects parallelization should be used
 - Result is an ‘unpartitioned mesh’
- Parallelization
 - Domain decomposition (cf. Lecture 3)
 - Solving ‘partitioned mesh’ in parallel
- Wide variety of different mesh types
 - Uniform meshes or non-uniform meshes
 - (also cf. Short Lecture 11 on visualization)

■ Mesh generation (aka grid generation) refers to generating a polygonal or polyhedral mesh that approximates a geometric domain and that is used in a wide variety of CFD and FEM simulations

[20] Wikipedia on Mesh



[21] T. Zwinger et al.

FEM – Adaptive Mesh Refinement (AMR)

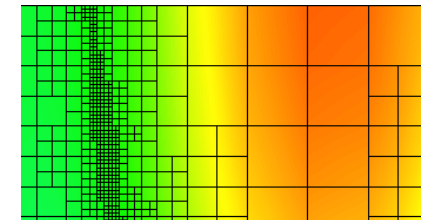
- Overcome ‘static mesh’ limits
 - ‘Discrete mesh’ spacing resolution simple approach in numerical analysis
 - No solutions of the numerical analysis on scales smaller than mesh spacing
 - AMR dynamically changes the spacing & shape of the mesh (i.e. dynamic grid)
 - Useful for very large range of scales
- Selected benefits
 - Increased computational savings over static grids
 - Flexible control of grid resolution as needed compared to the static grids or static mesh refinement
 - Increased storage savings over static grid

(static mesh refinement can be used for some regions that do not change shape over time)

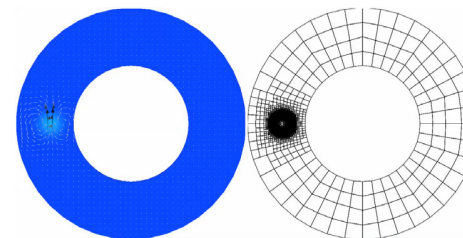
■ Adaptive mesh refinement (AMR) is a method in numerical analysis & HPC to dynamically change the accuracy of a solution in certain regions during the time the solution is calculated as simulation

modified from [22] Wikipedia on AMR

(use of adaptive mesh refinement as a method for reduction of big data outcomes of simulations)



(e.g. fire and heat transfer requires AMR as interesting regions vary over time)



[23] Civil Security & Traffic Group

FEM – AMR Fire Dynamics Simulator (FDS) – Application Example

■ Selected Facts

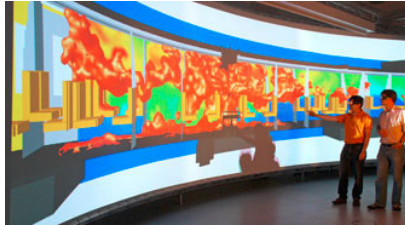
- Open source package
- Includes visualization tool SmokeView

■ Parallelization

- MPI (cf. Lecture 2) & OpenMP (cf. Lecture 6)
- Hybrid programming (cf. Lecture 10)
- Uses Adaptive Mesh Refinement (AMR)

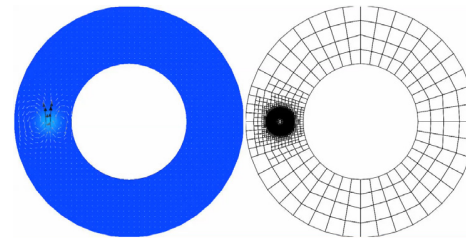
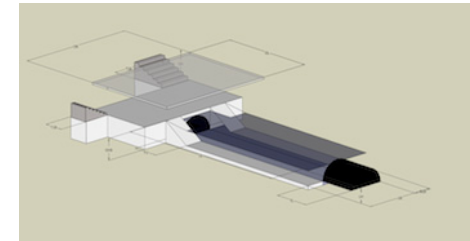
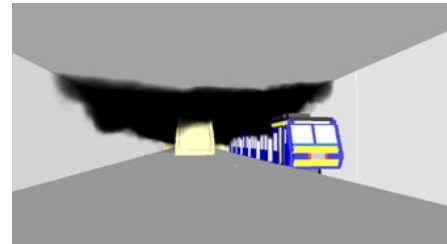
■ Examples

- Smoke and heat transport from fires in underground stations (e.g. fire safety / civil engineering)
- Fire simulations in trains, constructions, and generally objects



- Fire Dynamics Simulator (FDS) is a CFD simulation package solving simplified forms of the Navier-Stokes equations and enables large-eddy simulations (LES) for low-speed flows (i.e. smoke/fire)

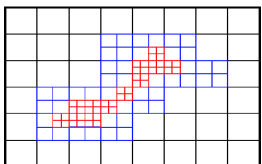
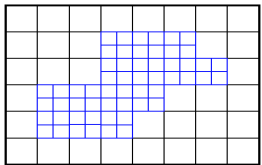
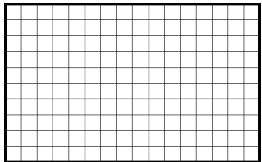
modified from [29] FDS Web page



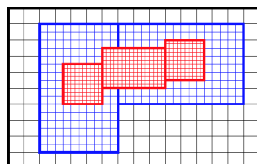
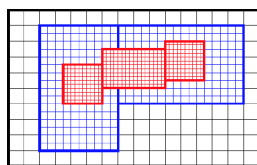
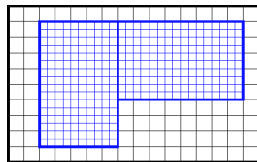
[23] Civil Security & Traffic Group

FEM – Adaptive Mesh Refinement – Tree-Code Example (cf. Lecture 5)

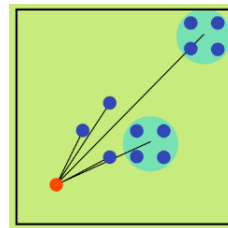
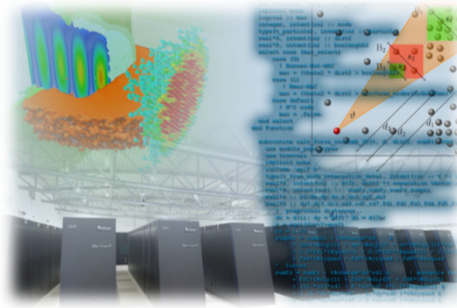
■ Different approaches



(point-based)



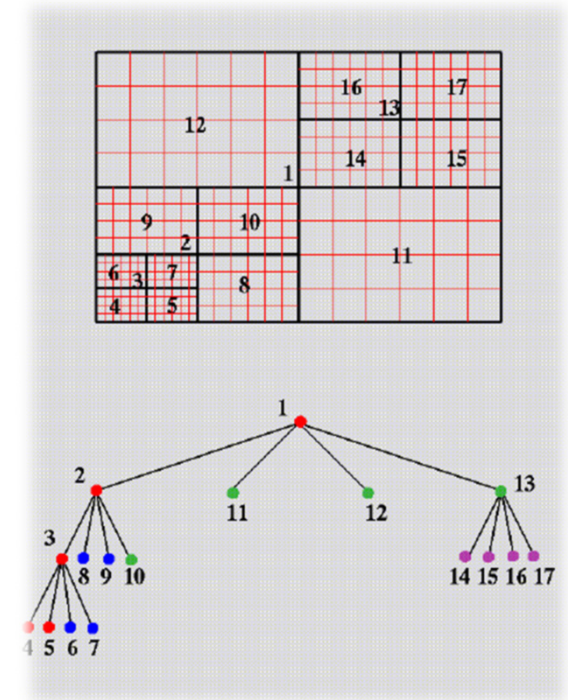
(patch-based)



[25] PEPC Web page

[26] F. Salvatore et al.

■ Often tree-based implementation

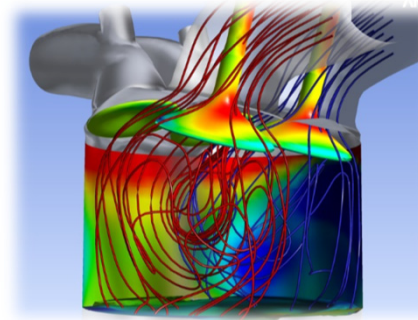


(block-based tree)

Selected Libraries & Methods – Ansys

■ Selected Facts

- Strong commercial software tools w.r.t. functionality (although commercial available at many HPC centers)
- Enables predictions how manufactured products will operate in real world
- Offers FEM, structural analysis, CFD, etc.

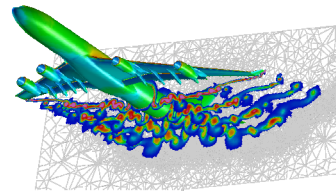


- Ansys is a commercial software package that consists of a wide variety of tools that enable HPC simulation-driven product development with several dedicated HPC packs & GPU support

modified from [34] Ansys Web page

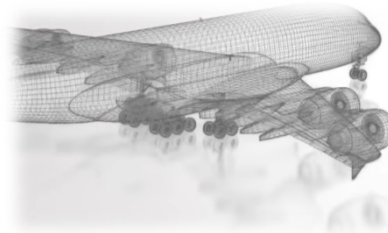
■ Parallelization

- Different ‘HPC packs’ across multiple physics problems packages
- GPU enabled (cf. Lecture 7) package
- Stores grids in HDF files (cf. Lecture 5)

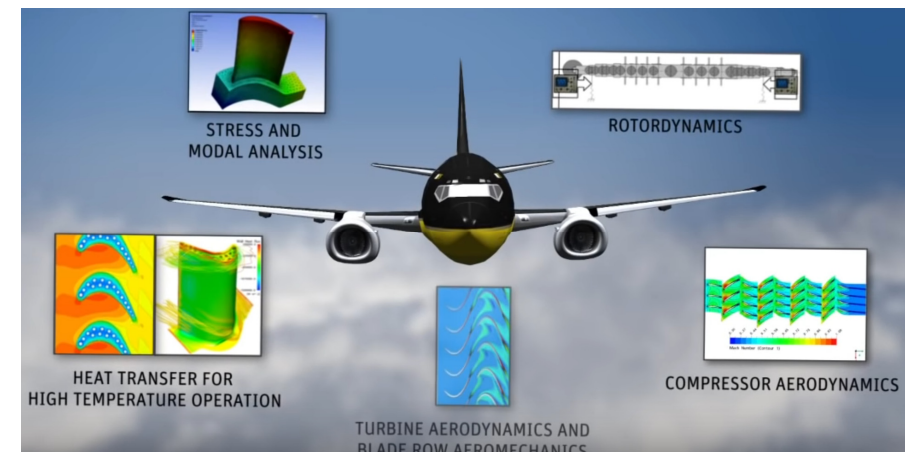


■ Example

- Internal combustion engine modeled using ANSYS Fluent
- Aerospace engineering



modified from [35] Ansys YouTube Video



Selected Libraries & Methods – OpenFOAM Revisited & Code_Aster

■ OpenFOAM Selected Facts

- Open source and many other features

■ OpenFOAM Parallelization

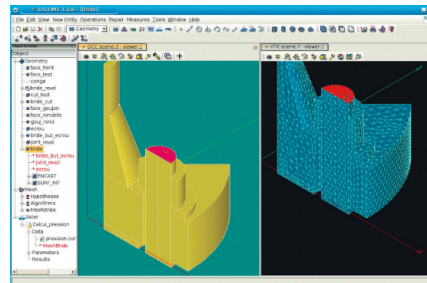
- Implementation of AMR (and coarsening)

■ OpenFOAM Example

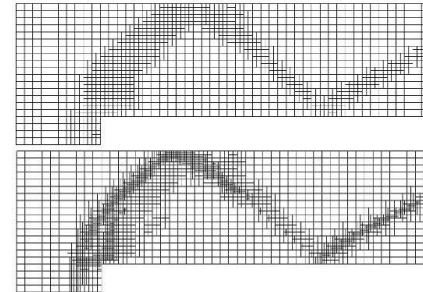
- Automatic resolution control for the finite volume method
- Error guides the refinement process & updates mesh

■ Code_Aster Selected Facts

- Free and open source software tool for FEM and related methods
- Integrated with Salome-Meca platform (GUI functions, visualization, etc.)



- Code_Aster offers a full range of multiphysical analysis and modelling approaches useful for computer aided engineering (CAE) and takes also partly advantage of parallelization methods

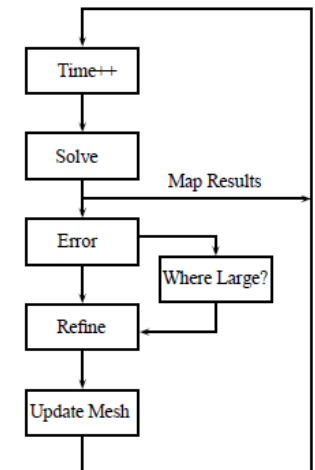
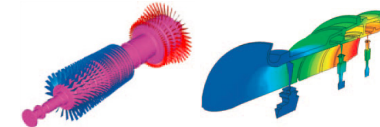


- Open source field operation & manipulation (OpenFOAM) is a C++ toolbox of numerical solvers & pre-/post processing utilities for the solution of CFD problems used in HPC simulations

modified from [32] OpenFOAM Web page

[36] OpenFOAM Tutorial

(automatically improve the accuracy of CFD and FEM simulations in interesting regions)



modified from [37] Code_Aster Manual

Selected Libraries & Methods – Elmer Package & Application Example

Selected Facts

- Open source multi-physical simulation software
- Includes physical models of structural mechanics, electromagnetics, heat transfer, acoustics, etc.
- Different tools ElmerGUI, ElmerSolver, ElmerPost

Parallelization

- Distributed memory with MPI (cf. Lecture 3)

Example

- Blood flow in carotid artery (poses a fluid-structure interaction challenge)
- Ice dynamic models (e.g. for ice calving)

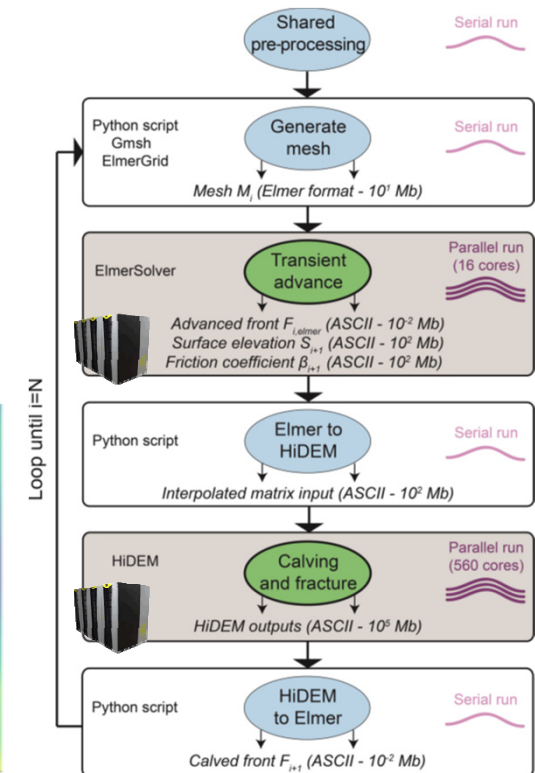
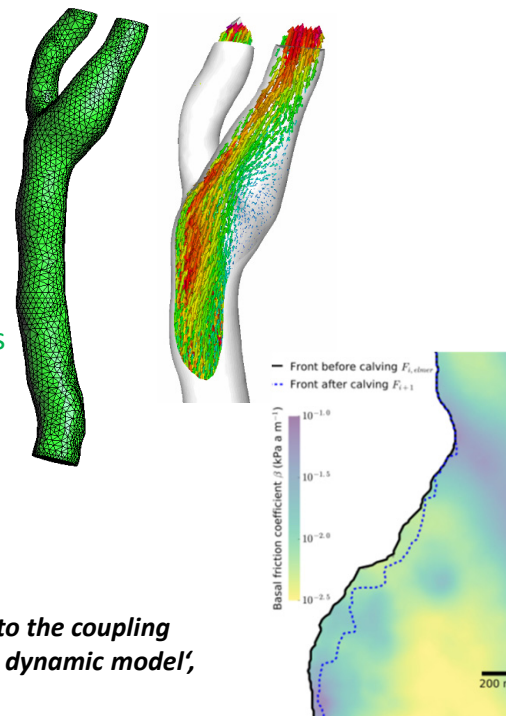
(e.g. research on calcification that reduces elasticity of arteries)

[24] Elmer Para2012 Tutorial

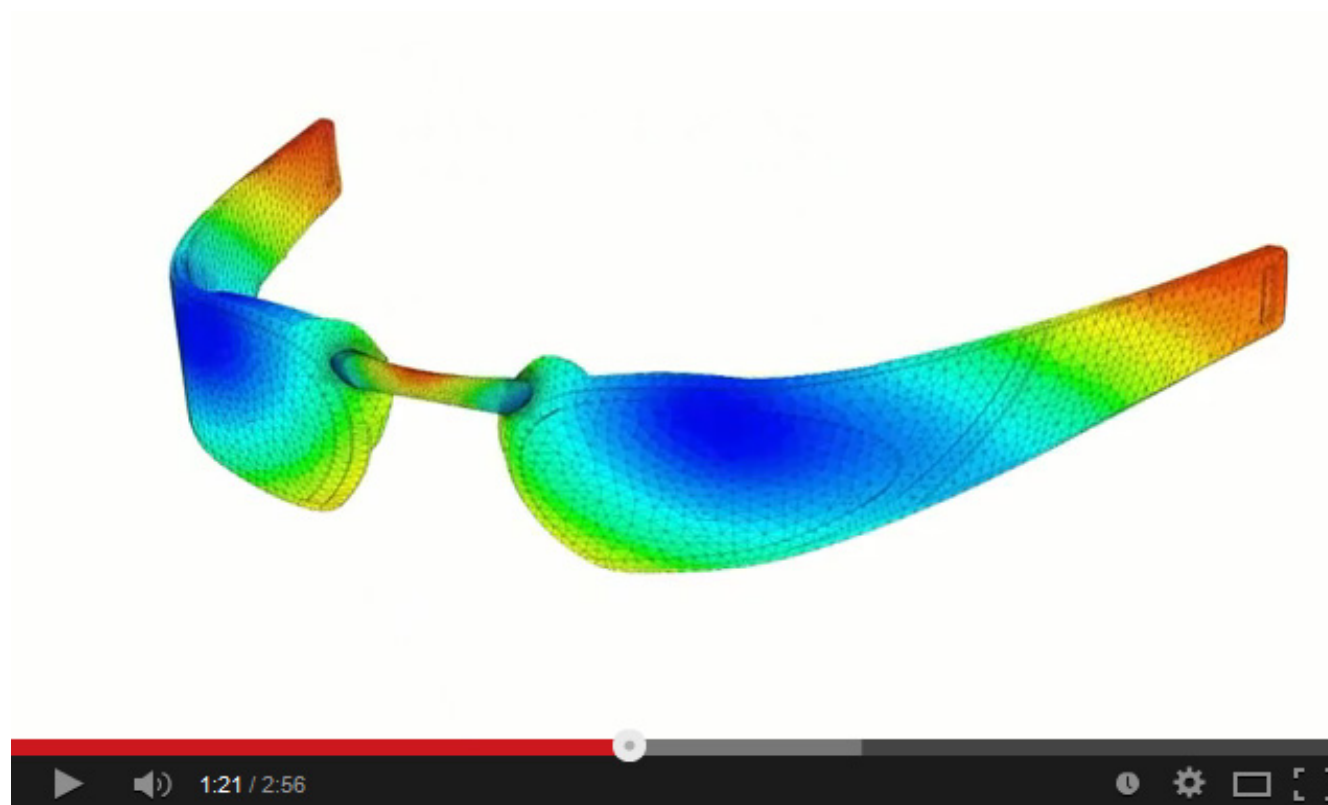
[30] M.S. Memon and M. Riedel et al., 'Scientific workflows applied to the coupling of a continuum (Elmer v8.3) and a discrete element (HiDEM v1.0) ice dynamic model', *Geoscientific Model Development (GMD)*, Vol 12 (7), 2019

- Elmer is an open source multi-physical simulation software package that solves physical models described by partial differential equations via FEM and is used in a wide variety of HPC simulations

modified from [28] Elmer Web page

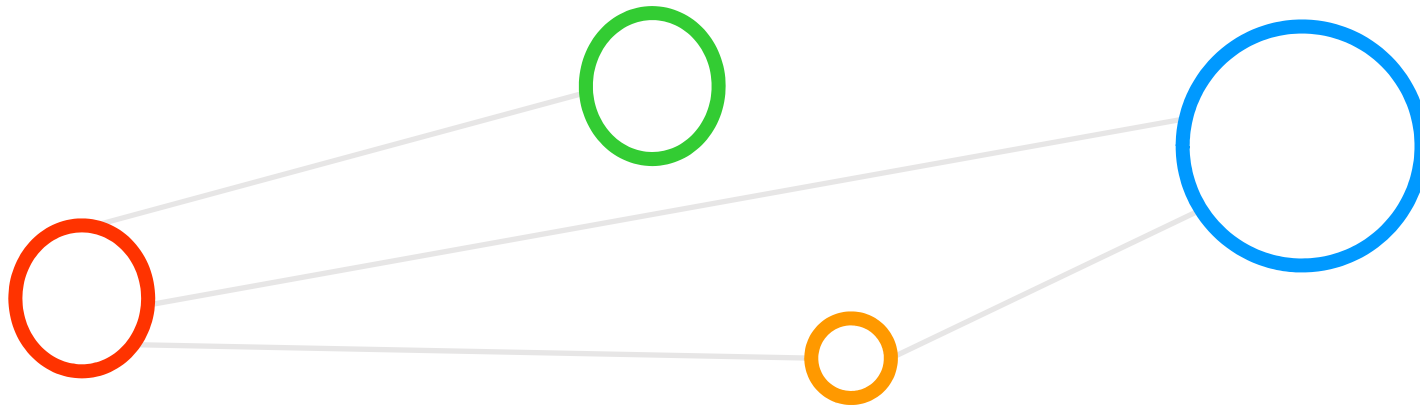


[Video] Speedo Application Use Case



[17] YouTube Video, 'Ansys Speedo Use Case'

Lecture Bibliography



Lecture Bibliography (1)

- [1] Wikipedia on 'Molecule', Online:
<http://en.wikipedia.org/wiki/Molecule>
- [2] Wikipedia on 'Atom', Online:
<http://en.wikipedia.org/wiki/Atom>
- [3] Wikipedia on 'Molecular Mechanics', Online:
http://en.wikipedia.org/wiki/Molecular_mechanics
- [4] Wikipedia on 'Molecular Docking', Online:
[http://en.wikipedia.org/wiki/Docking_\(molecular\)](http://en.wikipedia.org/wiki/Docking_(molecular))
- [5] Wikipedia on 'Molecular Dynamics', Online:
http://en.wikipedia.org/wiki/Molecular_dynamics
- [6] Hu Ge et al., 'Molecular Dynamics-Based Virtual Screening: Accelerating the Drug Discovery Process by High-Performance Computing' Journal of Chemical Information and Modeling 53(10), Online: https://www.researchgate.net/publication/256424059_Molecular_Dynamics-Based_Virtual_Screening_Accelerating_the_Drug_Discovery_Process_by_High-Performance_Computing
- [7] M. Riedel et al., 'Research Advances by using Interoperable e-Science Infrastructures', Journal of Cluster Computing, 12(4):357–372, 2009, Online: https://www.researchgate.net/publication/220405901_Research_advances_by_using_interoperable_e-science_infrastructures
- [8] Wikipedia on 'Computational Fluid Dynamics', Online:
http://en.wikipedia.org/wiki/Computational_fluid_dynamics
- [9] Folding@Home, Online:
<http://folding.stanford.edu/>
- [10] Steven Orszag et al., 'Lattice Boltzmann Methods for Fluid Dynamics', Online:
<http://physics.wustl.edu/nd/event/qmcd09/Presentations/qmcd09Talks/orszag.pdf>
- [11] Wikipedia on 'Navier-Stokes', Online:
http://en.wikipedia.org/wiki/Navier%E2%80%93Stokes_equations
- [12] Wikipedia on 'Lattice Boltzmann Methods', Online:
http://en.wikipedia.org/wiki/Lattice_Boltzmann_methods

Lecture Bibliography (2)

- [13] Wikipedia on 'Large eddy simulations', Online:
http://en.wikipedia.org/wiki/Large_eddy_simulation
- [14] Wikipedia on 'Turbulence', Online:
<http://en.wikipedia.org/wiki/Turbulence>
- [15] Wikipedia on 'stencil code', Online:
http://en.wikipedia.org/wiki/Stencil_code
- [16] YouTube Video, 'Computational Fluid Dynamics (CFD)', Online:
<http://www.youtube.com/watch?v=hzTCCcsOTg8>
- [17] YouTube Video, 'Ansys Speedo Use Case', Online:
<http://www.youtube.com/watch?v=H1EuTIhmAAA>
- [18] Wikipedia on 'Boundary Value Problems', Online:
http://en.wikipedia.org/wiki/Boundary_value_problem
- [19] Wikipedia on 'Finite Elements Method', Online:
http://en.wikipedia.org/wiki/Finite_element_method
- [20] Wikipedia on 'Mesh generation', Online:
http://en.wikipedia.org/wiki/Mesh_generation
- [21] Thomas Zwinger, 'Introduction into Elmer multiphysics FEM package', Online:
<http://websrv.cs.umd.edu/isis/images/e/e6/ElmerIntro.pdf>
- [22] Wikipedia on 'Adaptive Mesh Refinement', Online:
http://en.wikipedia.org/wiki/Adaptive_mesh_refinement
- [23] Civil Security & Traffice Group, Online:
http://www.fz-juelich.de/ias/jsc/EN/Research/ModellingSimulation/CivilSecurityTraffic/FireSimulation/Activities/_node.html
- [24] ELMER Para2012 Tutorial

Lecture Bibliography (3)

- [25] PEPC Web page, FZ Juelich, Online:
http://www.fz-juelich.de/ias/jsc/EN/AboutUs/Organisation/ComputationalScience/Simlabs/slpp/SoftwarePEPC/_node.html
- [26] F. Salvadore, 'Parallel algorithms for Partial Differential Equations', Online:
https://hpc-forge.cineca.it/files/ScuolaCalcoloParallelo_WebDAV/public/anno-2013/Summer-School/ParAlgo-slides-Rome.pdf
- [27] ELMER Scientific FEM code, Online:
<https://csc.fi/web/elmer>
- [28] ELMER Scientific FEM code, Online:
<https://csc.fi/web/elmer>
- [29] FDS Web page, Online:
<http://code.google.com/p/fds-smv/>
- [30] M.S. Memon and M. Riedel et al., 'Scientific workflows applied to the coupling of a continuum (Elmer v8.3) and a discrete element (HiDEM v1.0) ice dynamic model', Geoscientific Model Development (GMD), Vol 12 (7), 2019, Online:
https://www.researchgate.net/publication/326521081_ScientificWorkflows_Applied_to_the_Coupling_of_a_Continuum_Elmer_v83_and_a_Discrete_Element_HiDEM_v10_Ice_Dynamic_Model
- [31] Lohmeyer Consulting Engineers, Online:
<http://www.lohmeyer.de/en/node/529>
- [32] OpenFOAM Web page, Online:
<http://www.openfoam.com/>
- [33] P. Wenisch et al., 'Computational Steering: Interactive Flow Simulation in civil Engineering', inSiDE, Vol. 5(2),2007
- [34] Ansys Web page, Online:
<http://www.ansys.com/>
- [35] YouTube Video, 'Aerospace Industry Demands Accurate, Fast and Reliable Simulation Technology', Online:
<https://www.youtube.com/watch?v=otj39Zk1-aM>
- [36] Anton Berce, 'OpenFOAM Tutorial - Adaptive mesh refinement',
- [37] Code_Aster Manual, Online:
http://www.code-aster.org/V2/UPLOAD/DOC/Presentation/plaquette_aster_en.pdf

