

High Performance Computing

ADVANCED SCIENTIFIC COMPUTING

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LECTURE 6

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Parallel Programming with OpenMP

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UNIVERSITY OF ICELAND SCHOOL OF ENGINEERING AND NATURAL SCIE

FACULTY OF INDUSTRIAL ENGINEERING, MECHANICAL ENGINEERING AND COMPUTER SCIENCE









Review of Practical Lecture 5.1 – MPI Communicators & Data Structures

Example: Nearest Neighbour & Cartesian High-Level I/O Hierarchical Data Format (HDF)

```
MPI Init(&argc, &argv);
MPI Comm size(MPI COMM WORLD, &numtasks);
MPI Cart create (MPI COMM WORLD, 2, dims, periods,
            reorder, &cartcomm);
MPI Comm rank(cartcomm, &rank);
. . .
MPI Cart coords (cartcomm, rank, 2, coords);
MPI Cart shift(cartcomm, 0, 1,
            &nbrs[UP], &nbrs[DOWN] );
MPI Cart shift(cartcomm, 1, 1,
            &nbrs[LEFT], &nbrs[RIGHT]);
printf("rank= %d coords= %d %d" having
  neighbours (u, d, l, r) = d d d d d n",
```

```
rank, coords[0], coords[1],
nbrs[UP], nbrs[DOWN], nbrs[LEFT], nbrs[RIGHT]);
```

```
// do some work with MPI communication operations...
. . .
```

[morris@jotunn hpdbscan]\$ pwd /home/morris/2019-HPC-Course/hpdbscan [morris@jotunn hpdbscan]\$ ls -al total 1342196										
drwxrwxr-x	2	morris	morris	4096	okt	2	13:16			
drwxrwxr-x	12	morris	morris	4096	okt	2	20:21			
-rwxr-xr-x	1	morris	morris	1302382632	okt	2	13:16	bremen.h5		
-rwxr-xr-x	1	morris	morris	72002416	okt	2	20:40	bremenSmall.h5		
- rw- rw- r	1	morris	morris	Θ	okt	2	13:13	HPDBSCAN-199934.err		
- rw- rw- r	1	morris	morris	490	okt	2	13:14	HPDBSCAN-199934.out		
- rw- rw- r	1	morris	morris	Θ	okt	2	13:14	HPDBSCAN-199935.err		
- rw- rw- r	1	morris	morris	492	okt	2	13:17	HPDBSCAN-199935.out		
-rwxr-xr-x	1	morris	morris	535	okt	2	13:14	submit-clustering-bremen.sh		

BATCH -- iob-name=HPDBSCAN DBSCAN=dbscar

```
MENSMALLDATA=/home/morris/2019-HPC-Course/hpdbscan/bremenSmall.h5
EMENBIGDATA=/home/morris/2019-HPC-Course/hpdbscan/bremen.h5
```

mpirun \$HPDBSCAN -m 300 -e 500 \$BREMENSMALLDATA

[1] M. Goetz and M. Riedel et al, Proceedings IEEE Supercomputing Conference, 2015



HDF5 "bremenSmall.h5" { FILE CONTENTS {

/COLORS

/Clusters /DBSCAN

aroup

dataset

dataset

dataset

hpdbscan]\$ h5dump -n bremenSmall.

Outline of the Course

- 1. High Performance Computing
- 2. Parallel Programming with MPI
- 3. Parallelization Fundamentals
- 4. Advanced MPI Techniques
- 5. Parallel Algorithms & Data Structures
- 6. Parallel Programming with OpenMP
- 7. Graphical Processing Units (GPUs)
- 8. Parallel & Scalable Machine & Deep Learning
- 9. Debugging & Profiling & Performance Toolsets
- 10. Hybrid Programming & Patterns

- 11. Scientific Visualization & Scalable Infrastructures
- 12. Terrestrial Systems & Climate
- 13. Systems Biology & Bioinformatics
- 14. Molecular Systems & Libraries
- 15. Computational Fluid Dynamics & Finite Elements
- 16. Epilogue

+ additional practical lectures & Webinars for our hands-on assignments in context

- Practical Topics
- Theoretical / Conceptual Topics

Outline

- Shared-Memory Programming Concepts
 - OpenMP with Parallel & Serial Regions
 - Fork/Join & Master and Worker Threads
 - OpenMP Standard & Portability
 - Hybrid Programming Motivation & PyCOMPSs/COMPSs
 - OmpSs & OpenMP Data-Flow & Task-Based Evolutions
- OpenMP Parallel Programming Basics
 - Basic building blocks
 - Local/shared variables & Loops
 - Synchronization & Critical Regions
 - Selected Comparisons with MPI & Evolutions
 - HPDBSCAN Clustering OpenMP & Jacobi Application Example

- Promises from previous lecture(s):
- Lecture 1: Lecture 6 will give in-depth details on the shared-memory programming model with OpenMP and using its compiler directives
- Lecture 3: Lecture 6 will offer more elaborate shared memory parallel programming examples in context of different HPC application domains



Shared-Memory Programming Concepts



Shared-Memory Computers – Revisited (cf. Lecture 1)

A shared-memory parallel computer is a system in which a number of CPUs work on a common, shared physical address space

[2] Introduction to High Performance Computing for Scientists and Engineers

- Two varieties of shared-memory systems:
 - 1. Unified Memory Access (UMA)
 - 2. Cache-coherent Nonuniform Memory Access (ccNUMA)
- The Problem of 'Cache Coherence' (in UMA/ccNUMA)
 - Different CPUs use Cache to 'modify same cache values'
 - Consistency between cached data & data in memory must be guaranteed
 - 'Cache coherence protocols' ensure a consistent view of memory



Shared-Memory with UMA – Revisited (cf. Lecture 1)

MANY





Also called Symmetric Multiprocessing (SMP)

[2] Introduction to High Performance Computing for Scientists and Engineers





Selected Features

- Socket is a physical package (with multiple cores), typically a replacable component
- Two dual core chips (2 core/socket)
- P = Processor core
- L1D = Level 1 Cache Data (fastest)
- L2 = Level 2 Cache (fast)
- Memory = main memory (slow)
- Chipset = enforces cache coherence and mediates connections to memory

Shared-Memory with ccNUMA – Revisited (cf. Lecture 1)

- ccNUMA systems share logically memory that is physically distributed (similar like distributed-memory systems)
- Network logic makes the aggregated memory appear as one single address space

[2] Introduction to High Performance Computing for Scientists and Engineers



Selected Features

- Eight cores (4 cores/socket); L3 = Level 3 Cache
- Memory interface = establishes a coherent link to enable one 'logical' single address space of 'physically distributed memory'

Programming with Shared Memory using OpenMP – Revisited (cf. Lecture 1)

- Shared-memory programming enables immediate access to all data from all processors without explicit communication
- OpenMP is dominant shared-memory programming standard today
- OpenMP is a set of compiler directives to 'mark parallel regions'

[3] OpenMP API Specification

Features

- Bindings are defined for C, C++, and Fortran languages
- Threads TX are 'lightweight processes' that mutually access data



(uniform memory access)



(non-uniform memory access)



Lecture 6 – Parallel Programming with OpenMP

[7] LLNL OpenMP Tutorial

What means a 'Shared Address Space'?

- Shared-memory programming enables immediate access to all data from all processors without explicit communication
- OpenMP is dominant shared-memory programming standard today
- OpenMP is a set of compiler directives to 'mark parallel regions'

[3] OpenMP API Specification



(programming model: work on shared address space – 'local acess to memory')

What is OpenMP?

- OpenMP is a library for specifying 'parallel regions in serial code'
 - Defined by major computer hardware/software vendors → portability!
 - Enable scalability with parallelization constructs w/o fixed thread numbers
 - Offers a suitable data environment for easier parallel processing of data
 - Uses specific environment variables for clever decoupling of code/problem
 - Included in standard C compiler distributions (e.g. gcc)
- Threads are the central entity in OpenMP
 - Threads enable 'work-sharing' and share address space (where data resides)
 - Threads can be synchronized if needed
 - Lightweight process that share common address space with other threads
 - Initiating (aka 'spawning') n threads is less costly then n processes (e.g. variable space)



[3] OpenMP API Specification



- Recall 'computing nodes' are <u>independent</u> computing processors (that may also have N cores each) and that are all part of one big parallel computer
- Threads are lightweight processes that work with data in memory

Important Terminology



- Thread: An execution entity with a stack and associated static memory, called thread private memory
- OpenMP Thread: A thread that is managed by the OpenMP runtime system
- Team: A set of one or more threads participating in the execution of a parallel region
- Task: A specific instance of executable code and its data environment that the OpenMP imlementation can schedule for execution by threads
- Base Language: A programming language that serves as the foundation of the OpenMP specification
- Base Program: A program written in the base language
- OpenMP Program: A program that consists of a base program that is annotated with OpenMP directives or that calls OpenMP API runtime library routines.
- Directive: In C/C++, a #pragma that specifies OpenMP program behavior



[3] OpenMP API Specification

Understanding Parallel & Serial Regions



OpenMP Standard enables Portability

- Key reasons for requiring a standard programming library
 - Technical advancement in supercomputers is extremely fast
 - Parallel computing experts switch organizations and face another system
- Applications using proprietary libraries where not portable
 - Create whole applications from scratch or time-consuming code updates
- OpenMP is parallel programming model for UMA and ccNUMA



- OpenMP is an open standard that significantly supports the portability of parallel shared-memory applications
- But different vendors might implement it differently

Programming Hybrid Systems – Motivation

- Inefficient 'on-node communications' when using MPI instead of OpenMP
 - MPI uses 'buffering techniques' to transfer data (cf. Lecture 2 & 4)
 - Transfers may require 'multiple memory copies' to get data from A to B
 - Comparable to a 'memory copy' between different MPI processes
- Take advantage of shared memory techniques where feasible
 - OpenMP threads can read memory on the same node



Modified from [2] Introduction to High Performance Computing for Scientists and Engineers

Hierarchical Hybrid Computers – Revisited (cf. Lecture 1)

- A hierarchical hybrid parallel computer is neither a purely shared-memory nor a purely distributed-memory type system but a mixture of both
- Large-scale 'hybrid' parallel computers have shared-memory building blocks interconnected with a fast network today



[2] Introduction to High Performance Computing for Scientists and Engineers

Features

- Shared-memory nodes (here ccNUMA) with local NIs
- NI mediates connections to other remote 'SMP nodes'

> Lecture 10 will provide insights into hybrid programming models and introduces selected patterns used in parallel programming

Programming Hybrid Systems & Patterns – Revisited (cf. Lecture 1)

- Hybrid systems programming uses MPI as explicit internode communication and OpenMP for parallelization within the node
- Parallel Programming is often supported by using 'patterns' such as stencil methods in order to apply functions to the domain decomposition
- Experience from HPC Practice
 - Most parallel applications still take no notice of the hardware structure
 - Use of pure MPI for parallelization remains the dominant programming
 - Historical reason: old supercomputers all distributed-memory type
 - Use of accelerators is significantly increasing in practice today
- Challenges with the 'mapping problem'
 - Performance of hybrid (as well as pure MPI codes) depends crucially on factors not directly connected to the programming model
 - It largely depends on the association of threads and processes to cores
 - Patterns (e.g., stencil methods) support the parallel programming

P1 P2 P3 P4 P4



> Lecture 10 will provide insights into hybrid programming models and introduces selected patterns used in parallel programming

Programming Hybrid Systems with MPI & OpenMP

- Hybrid systems programming uses MPI as explicit internode communication and OpenMP for parallelization within the node
- Parallel Programming is often supported by using 'patterns' such as stencil methods in order to apply functions to the domain decomposition



[7] LLNL OpenMP Tutorial



Scientific Application Example: Data Mining & Clustering

- Hybrid data mining algorithm example
 - Parallel Density-based Spatial Clustering for Applications with Noise (DBSCAN)
 - Using MPI and OpenMP to scale better
 - Standalone OpenMP is also possible to use





location executable
HPDBSCAN=/homea/hpclab/train001/tools/hpdbscan/dbscan

your own copy of bremen small
BREMENSMALLDATA=/homea/hpclab/train001/bremenSmall.h5

your own copy of bremen big BREMENBIGDATA=/homea/hpclab/train001/bremen.h5

srun \$HPDBSCAN -m 100 -e 300 -t 12 \$BREMENSMALLDATA







[1] M. Goetz and M. Riedel et al, Proceedings IEEE Supercomputing Conference, 2015

Many-core GPGPUs – Revisited (cf. Lecture 1)

- Use of very many simple cores
 - High throughput computing-oriented architecture
 - Use massive parallelism by executing a lot of concurrent threads slowly
 - Handle an ever increasing amount of multiple instruction threads
 - CPUs instead typically execute a single long thread as fast as possible
- Many-core GPUs are used in large clusters and within massively parallel supercomputers today
 - Named General-Purpose Computing on GPUs (GPGPU)
 - Different programming models emerge



- Graphics Processing Unit (GPU) is great for data parallelism and task parallelism
- Compared to multi-core CPUs, GPUs consist of a many-core architecture with hundreds to even thousands of very simple cores executing threads rather slowly

DEEP-EST EU Project – OmpSs & OpenMP Evolutions

- OmpSs is an innovative programming model influencing OpenMP
 - Based on tasks and (data) dependencies tasks as elementary unit of work
 - Extend OpenMP model: better data-flow & heterogenity (e.g. GPGPUs)
 - New Version: OmpSs-2

[11] OmpSs Web Page







[9] Distributed & Cloud Computing Book



[10] DEEP Projects Web Page

OmpSs Programming Model – Adding Task & Data Dependencies



OmpSs main goal is to act as a forefront and nursery of ideas for a data-flow task-based programming model so these ideas can ultimately be incorporated in the OpenMP industrial standard

[12] OmpSs BSC Programming Models

Enabling Parallelization Approaches with Task Multi-Dependencies



[13] MontBlanc OmpSs Multi-Task Dependencies

COMPSs & PyCOMPSs

- COMPSs (COMP Superscalar)
 - Coarse-grained programming model oriented to distributed environments
 - Powerful runtime that leverages low-level APIs (e.g., Amazon EC2 clouds)
 - Manages data dependencies (objects and files)
 - COMP Superscalar (COMPSs) is a framework which aims to ease the development and execution of applications for distributed infrastructures, such as Clusters, Grids and Clouds.
 - PyCOMPSs is the Python binding of COMPSs
 - PyCOMPSs follows OpenMP & OmpSs approach: from a sequential Python code, it is able to run in parallel and distributed



pycompss.api.task import task rom pycompss.api.parameter import FILE_INOUT task(filePath = FILE_INOUT) ef increment(filePath): # Read value fis = open(filePath, 'r') value = fis.read() fis.close() # Write value fos = open(filePath, 'w') fos.write(str(int(value) + 1)) fos.close() f main_program(): from pycompss.api.api import compss_open # Check and get parameters if len(sys.argv) != 2: exit(-1)initialValue = sys.argv[1] fileName="counter

Lecture 6 - Parallel Programming with OpenMP



[14] PyCOMPSs

[Video] Scientific Application Example using OpenMP



[4] Lattice Boltzmann – Flow past an obstacle, YouTube Video

OpenMP Parallel Programming Basics



Start 'Thinking' Parallel

- Parallel OpenMP program
 - Knows about the existence of a certain number of threads that all work togeter as part of a bigger picture
- OpenMP programs
 - Written in a sequential programming language and some parts are executed in parallel
 - Run on a processor that 'spawns' numerous threads
- Parallelization
 - Dedicated n parallel regions is key to the design in OpenMP (n = 1,2,3....)
 - E.g. loops/additions are good candidates for parallelization
 - (if individual loop iterations are independent from each other)
- Start with the basic building blocks using OpenMP
 - Defining code that enables 'parallel computing', step-by-step is possible



Number of Threads & Scalability

- The real number of threads normally not known at compile time
 - (There are methods for doing it in the program \rightarrow do not use them!)
 - Number is set in scripts and/or environment variable before executing
 - Parallel programming is done without knowing number of threads

- OpenMP programs should be always written in a way that it does not assume a specific number of threads that in turn enables a scalable program
- Compiler directives are used such as #pragma omp parallel



OpenMP Basic Building Blocks: Hello World Example



Edit C Program with OpenMP Directives & Functions & Compilation

- Using basic gcc compiler
 - 'module load gnu openmpi'
 - Note: there are many C compilers available, we here pick one for our particular HPC course that works with OpenMP
 - Note: If there are no errors, the file hellothreads is now a full C program executable that can be started by an OS





С

hellothreads

executable

gcc -fopenmp



[1] Icelandic HPC Machines & Community

OpenMP Work Sharing Constructs – Overview



[7] LLNL OpenMP Tutorial

Data Parallelism: Medium-grained Loop Parallelization (cf. Lecture 3)

- Idea: Computations performed on individual array elements are independent of each other
 - Good for parallel execution by N processors (e.g., using shared memory parallel programming)





OpenMP Work Sharing Construct: Simple For Loop Example



OpenMP Work Sharing Construct: Advanced For Loop Example



OpenMP Work Sharing Construct: Sections Example



OpenMP Synchronization Construct: Critical Region Example

Memory



- If a thread is currently executing inside a critical region and another thread reaches that critical region and attempts to execute it, it will block until the first thread exits that critical region
- All threads in the team will attempt to execute in parallel, however, because of the critical construct surrounding the increment of x, only one thread will be able to read/increment/write x at any time
- Note the 'race conditions' of variable x otherwise: Race Condition in shared-memory: shared variable x will be set concurrently by the different threads – not with critical regions



OpenMP ThreadPrivate Directive – Persistence between Parallel Regions (1)



OpenMP ThreadPrivate Directive – Persistence between Parallel Regions (2)

<pre>#include <omp.h></omp.h></pre>
int a, b, i, tid;
float x;
<pre>#pragma omp threadprivate(a, x)</pre>
<pre>main(int argc, char *argv[]) {</pre>
<pre>printf("Master thread doing serial work here\n");</pre>
<pre>printf("2nd Parallel Region:\n");</pre>
<pre>#pragma omp parallel private(tid)</pre>
{
<pre>tid = omp_get_thread_num();</pre>
<pre>printf("Thread %d: a,b,x= %d %d %f\n",tid,a,b,x);</pre>
<pre>} /* end of parallel region */</pre>
}

Output:

1st Para	allel	Region	::							
Thread	0:	a,b,x=	0	0	1.	00	000	0		
Thread 2	2:	a,b,x=	2	2	3.	20	000	0		
Thread	3:	a,b,x=	3	3	4.	30	000	0		
Thread	1:	a,b,x=	1	1	2.	10	000	0		
******	****	******	**	**	**	**	***	**	***	*
Master	threa	d doing	r s	er	ia	1	wor	k	her	e
******	****	******	**	**	**	**	***	**	***	*
2nd Para	allel	Region	.:							
Thread	0:	a,b,x=	0	0	1.	00	000	0		
Thread	3:	a,b,x=	3	0	4.	30	000	0		
Thread	1:	a,b,x=	1	0	2.	10	000	0		
Thread 2	2:	a,b,x=	2	0	3.	20	000	0		

[7] LLNL OpenMP Tutorial

OpenMP Reduction Clause Example – Vector Dot Product Example



Selected Comparisons with MPI

- Some aspects are similar, because both enable parallel computing
 - Obtaining unique IDs: MPI ranks vs. OpenMP thread-num
 - Master-worker approach (if rank==0 vs. if tid ==0)
- No explicit communication constructs to enable inter-process communication in OpenMP → assuming shared-memory
 - Data exchange: Message exchanges between processes vs. shared variable
 - Synchronization functions nevertheless exist in both: e.g. barriers
 - Clever automatisms for usual problems: MPI reduce vs. OpenMP reduction





Recent Support of OpenMP for Programming GPUs with Directives



Lecture 7 will offer more details on OpenMP relationships of programming GPUs and similiarites to GPU programming using OpenACC

Monitoring, Debugging and Performance Analysis Tools for OpenMP

- Different Tools exist
 - E.g. TotalView Debugger
 - E.g. Linux top command

CMD

a.out

a.out

a.out

a.out

a.out

E.g. Linux ps command

% ps -:	Lf								
UID	I	PID.	PPID	LWP	С	NLWP	STIME	TTY	TIME
blaise	225	529	28240	22529	0	5	11:31	pts/53	00:00:00
blaise	225	529	28240	22530	99	5	11:31	pts/53	00:01:24
blaise	225	529	28240	22531	99	5	11:31	pts/53	00:01:24
blaise	225	529	28240	22532	99	5	11:31	pts/53	00:01:24
blaise	225	529	28240	22533	99	5	11:31	pts/53	00:01:24
* ns -'	Ψ								
PTD	SPTD	ጥጥን	,	TT:	IME	CMD			
22529	22529	pts	- s/53	00:00	:00	a.out	5		
22529	22530	pts	\$/53	00:01	:49	a.out			
22529	22531	pts	\$/53	00:01	:49	a.out			
22529	22532	pts	\$/53	00:01	:49	a.out	5		
22529	22533	pts	\$/53	00:01	: 49	a.out	-		
* ns -	T.m								
PID	LWP	TTY	,	т	IME	CMD			
22529		pts	- s/53	00:18	: 56	a.out	-		
- :	22529	-	.,	00:00	:00	_	-		
	22530	-		00:04	:44	-			
-	22531	-		00:04	: 44	-			
-	22532	-		00:04	: 44	-			
_	22533	-		00.04	• • •	-			



<u>F</u> ile	<u>E</u> dit	<u>V</u> iew	Terminal	Ta <u>b</u> s	<u>H</u> elp

top - 14:13:21 up 2 days, 23:17, 20 users, load average: 3.34, 1.59, 0.73 Tasks: 471 total, 5 running, 465 sleeping, 1 stopped, 0 zombie Cpu(s): 33.4%us, 1.7%sy, 0.0%ni, 56.6%id, 8.0%wa, 0.2%hi, 0.0%si, 0.0%st Mem: 24479116k total, 19015304k used, 5463812k free, 117572k buffers Swap: 4096564k total, 89432k used, 4007132k free, 16511060k cached

PID	USER	PR	NI	VIRT	RES	SHR	S	%CPU %	6 ME M	TIME+ COMMAND
18010	blaise	25	0	92292	1248	920	R	100.0	0.0	0:42.68 a.out
18012	blaise	25	0	92292	1248	920	R	100.0	0.0	0:42.62 a.out
18013	blaise	25	0	92292	1248	920	R	100.0	0.0	0:42.65 a.out
18014	blaise	25	0	92292	1248	920	R	99.7	0.0	0:42.61 a.out
617	root	15	0	0	0	0	D	1.3	0.0	0:15.36 pdflush
4344	root	15	0	0	0	0	s	0.7	0.0	1:37.12 kiblnd_sd_02
4345	root	15	0	0	0	0	S	0.7	0.0	1:38.24 kiblnd_sd_03
4352	root	15	0	0	0	0	S	0.7	0.0	1:37.56 kiblnd_sd_10
5055	root	15	0	0	0	0	S	0.7	0.0	10:19.15 ptlrpcd

[7] LLNL OpenMP Tutorial

> Lecture 9 will provide a set of tools that can be used for monitoring, debugging, and performance analysis of MPI and OpenMP

Jacobi 2D Application Example – Shared Memory with OpenMP Possible

Solver

- Each diagonal element is solved and approximate value is plugged in
- The process is iterated until it converges
- Update function 2D Jacobi iterative method example
 - E.g. computes the arithmetic mean of a cell's four neighbours
 - E.g. solving diffusion equations (heat dissipation example)



[2] Introduction to High Performance Computing for Scientists and Engineers

Lecture 10 will provide more details about stencil-based iterative methods & used patterns in many different HPC application examples

'stencil code'

- The Jacobi iterative method is a stencil-based iterative method used in numerical linear algebra
- Algorithm for determining the solutions of diagonally dominant system of linear equations



'Big Data' Science Example – Parallel & Scalable Clustering Algorithm – Revisited



Lecture 6 – Parallel Programming with OpenMP

512

2

0 2

HPDBSCAN Clustering OpenMP Application Example in Data Sciences



[1] M. Goetz and M. Riedel et al, Proceedings IEEE Supercomputing Conference, 2015

[Video] Raytracing Application with OpenMP



[6] Speeding up a Ray tracer with OpenMP, YouTube Video

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